HINGES AND ROTATIONS

Before the three modules are hinged together, they are sectioned into a total of six identical modules. This further division is helpful when the three finished modules do not fit back together physically, usually because of collisions due to undercuts in the design of the section.



Fig. 16 — The 1/3 module split in half. The resulting 1/6 modules are identical and right-handed.

Fig. 16b - In a typical chain constructed by Scarpa and illustrated in his book, "pairs" of symmetrical modules form the basic structure of the chain. The modules are repeated and hinged together along symmetry axes (Modelli, page 62).

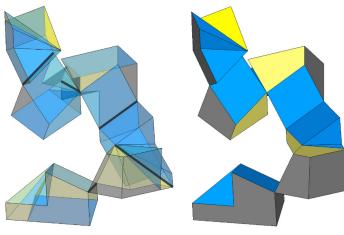
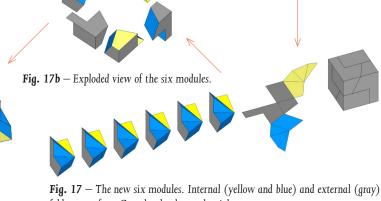


Fig. 18 — The six modules have been hinged along the cube's half diagonals and other segments on the faces. The hinges are shown as dark thick lines in the view on the left. Four such groups are connected together in the "closed-chain" configuration used for the model seen in Fig. 19 and Fig. 20.



fold-out surface. Completed cube on the right.

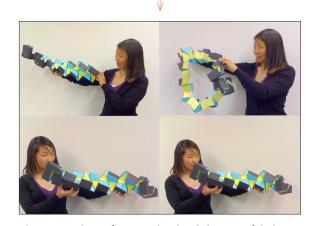
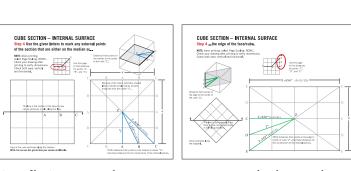


Fig. 19 — In this configuration the selected placement of the hinges produced a closed chain where the modules cannot fold back into their minimal volume of 2 x 2 x 1 cubes. Chain is composed of 24 identical modules. Each module occupies 1/6 of one cube. Four complete cubes compose the chain. Model by Florence Gold Yuen, SFSU.



Appendix A — Diagrams showing geometric construction used to determine the internal measurements of the modules

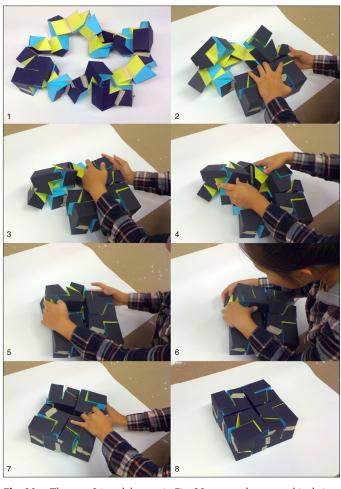
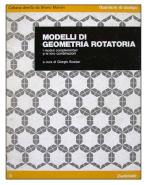


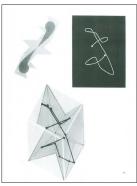
Fig. 20 — The same 24 modules seen in Fig. 29 were used to create this chain, which folds back into the minimum volume of 2 x 2 x 1 cubes. The location and spatial orientation of the hinges needs to be formalized and mapped. We can expand this configuration into a larger volume composed of eight cubes, having 48 modules hinged together in a similar sequence. Model by Florence Gold Yuen, SFSU.

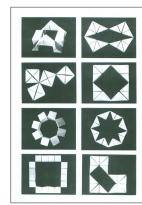
ROTATIONAL GEOMETRY AS A TEACHING TOOL: APPLYING THE WORK OF GIORGIO SCARPA

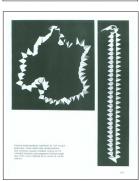
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Giorgio Scarpa, Modelli di Geometria Rotatoria [Models of Rotational Geometry . Bologna: Zanichelli, 1978. Cover and sample pages: 43, 77, 107.

Genesis of form. Motion is at the root of all growth — Paul Klee

Although rotational geometry is a difficult field of mathematics available only to specialists, the physical models that apply its principles are highly useful for courses in sketching and drawing. Students at San Francisco State University have found rotational geometry to be one of the most valuable segments of the drawing course, offering such remarks as: "I feel that this project used all of the skills that we learned in class, from drawing the basic shape in orthographic and axonometric views to the cubic modules in perspective." "This project challenged my design thinking by taking a 2D object and rendering it in a 3D environment."

I was able to teach this segment of the course thanks to the teaching and writings of the Italian scholar Giorgio Scarpa (1938-2012). This presentation introduces his work to English-speaking specialists, and illustrates how the subject can be made useful to design students.

Giorgio Scarpa taught Descriptive Geometry at the Istituto d'Arte of Oristano and Faenza, Italy, and Theory of Perception at the Istituto Superiore Industrie Artistiche (ISIA) in Faenza. His book Modelli di Geometria Rotatoria, which was part of a design series edited by Italian designer Bruno Munari, is the basis of this study. This teaching unit in drawing for design uses and applies Scarpa's principles and methods, and tests their validity through the construction of physical models built by the students. Through this process, students learn to apply a visual grammar based on rotational movements and folding which transform twodimensional shapes into three-dimensional solids. These solids are modules derived from the sectioning of regular polyhedra such as the cube. In theory, any regular polyhedron

can be used as the basis for the section. In this study only the cube is used, due to its simple, intuitive symmetry.

Drafting and Sketching for Design is a required course for all students entering the Design and Industry Department at San Francisco State University. In the class, all drawing is done by hand with drafting tools and free hand sketching. The class covers orthographic projections, axonometric projections, and perspective. These techniques are also explored within a unit called Cube Section.

The unit begins with the simple problem: dissect a 4" x 4" x 4" cube into two or three solid modules (polyhedra), having identical surface area, volume, and shape. The threedimensional modules that will form the final cube can be connected at a later time by means of hinges. The connected modules can be arranged into open or closed chains. The modules may or may not fold back into a minimum volume enclosure depending on the type and orientation of the hinges used. The materials used in this process are pencil, paper and tape or glue.

While the students are able to improve their manual skills through the use of these materials, the alternative use of CAD and rapid prototyping tools would allow for faster testing of the various configurations.

We'll call the process for the section that divides the cube into two modules the "twin" section. The process that divides the cube into three modules will be called the "triplet"

Text and images in this handout are adapted from the paper by the same title. More details can be found at the URLs below. Thank you.

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Giorgio Scarpa — online.sfsu.edu/trogu/scarpa Cube section — online.sfsu.edu/sketch/cube This handout and slides - troqu.com/Documents/conference/2013_drs_cumulus_oslo

Fig.7a — Internal surface.

Fig. 7b — Orthographic views.

Fig. 7c and **7d** — Isometric views of the modules.

Fig. 9c — This new continuous

four-part shape occupies exactly

one third of the external surface

of the cube. Common boundaries

(thick lines in the illustration)

will be folded 90° in 3D space.

Fig. 15b - Actual modules built with card stock. A combination of blue

and yellow board

is used later in the

six-module version

of this cube.

and right-handed. Completed cube at right.