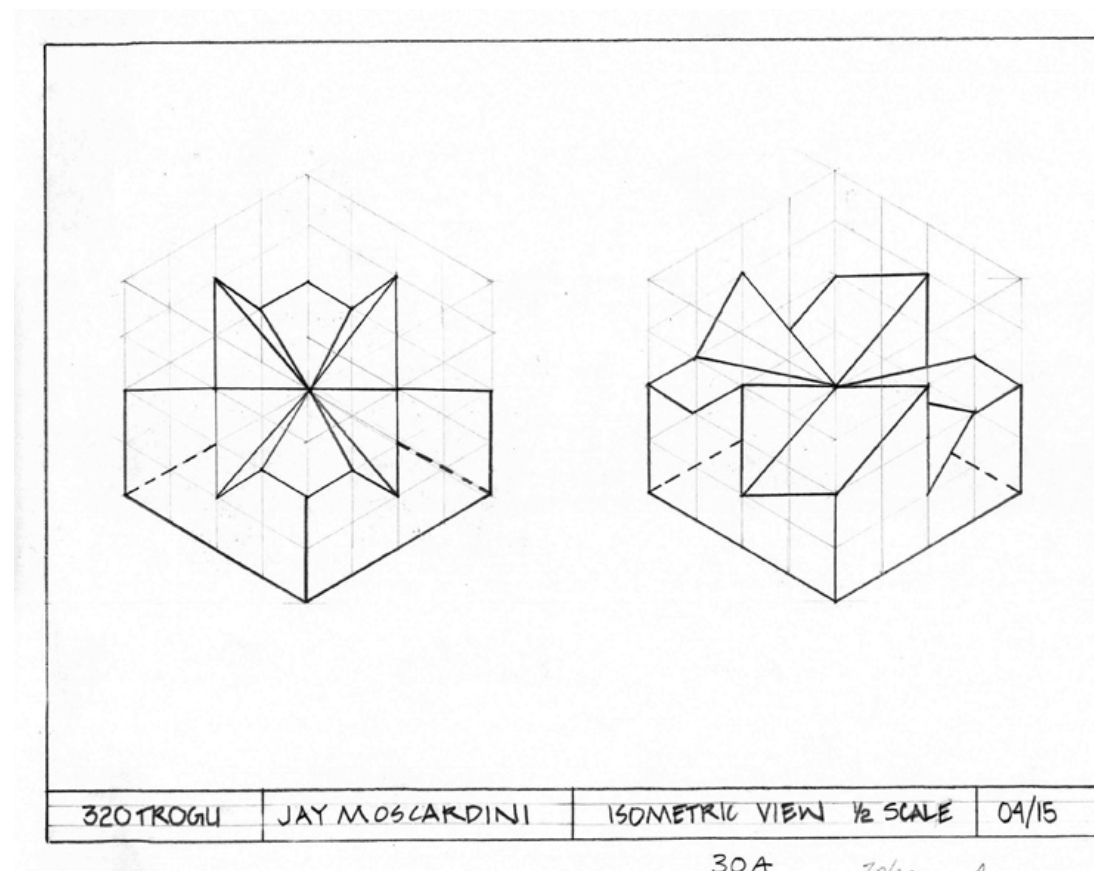


# ROTATIONAL GEOMETRY AS A TEACHING TOOL : APPLYING THE WORK OF GIORGIO SCARPA

PINO TROGU – SAN FRANCISCO STATE UNIVERSITY

SIXTH INTERNATIONAL CONFERENCE ON DESIGN PRINCIPLES AND PRACTICES

LOS ANGELES, JANUARY 21, 2012



[go to last slide](#)



## Quaderni di design

La collana, dedicata in particolare a insegnanti e studenti di educazione tecnica, educazione artistica e design, è un prezioso e stimolante strumento di consultazione per chiunque si interessi alla formazione della cultura di oggi.

I singoli volumi, ampiamente illustrati, hanno per argomento i punti nodali della progettazione: la raccolta dei dati, la sperimentazione, l'aspetto fisico e psicologico del progetto, l'informazione culturale e tecnologica relativa a materie e strumenti, la metodologia progettuale, la costruzione di modelli, l'indagine su forme e fenomeni naturali, le regole di coerenza formale, il linguaggio tecnico e la comunicazione visiva.

### Nella collana

- 1 Textures  
a cura di Corrado Gavinelli
- 2 La scoperta del triangolo  
a cura di Bruno Munari
- 3 Ricerca e progettazione di un simbolo  
a cura di Pietro Gasperini
- 4 Xerografie originali  
a cura di Bruno Munari
- 5 Modelli di geometria rotatoria  
a cura di Giorgio Scarpa
- 6 La scoperta del quadrato  
a cura di Bruno Munari

### In preparazione

- 7 Colore: codice e norma  
a cura di Narciso Silvestrini
- 8 La scoperta del pentagono  
a cura di Aldo Montù

Sezionare una forma basilare, un quadrato o un triangolo, in due o più pezzi, ruotare questi pezzi sul piano fino a combinarli in altro modo: si ottengono nuove forme che, a loro volta si combinano con altre simili. Da tutte queste combinazioni e rotazioni di elementi di forme nascono ancora altre forme che, a prima vista sembrano molto complesse, in realtà tutto diventa molto semplice, quando si conosce la regola. Giorgio Scarpa mostra in questo libro tutti i procedimenti logici per ottenere nuove forme a due e a tre dimensioni. La conoscenza di questi processi aiuta la formazione di un pensiero progettuale più attivo e, inoltre, fa capire meglio certi aspetti di forme naturali nate dalla rotazione di elementi modulati. L'arancia è una sfera la cui forma nasce dalla rotazione dei moduli a forma di spicchio, attorno a un asse rettilineo.

33E0042 OD 05 Scarpa Modelli geom. rotatoria

ZANICHELLI EDITORE  
Prezzo al pubblico  
I.V.A. inclusa £15.000

Collana diretta da Bruno Munari

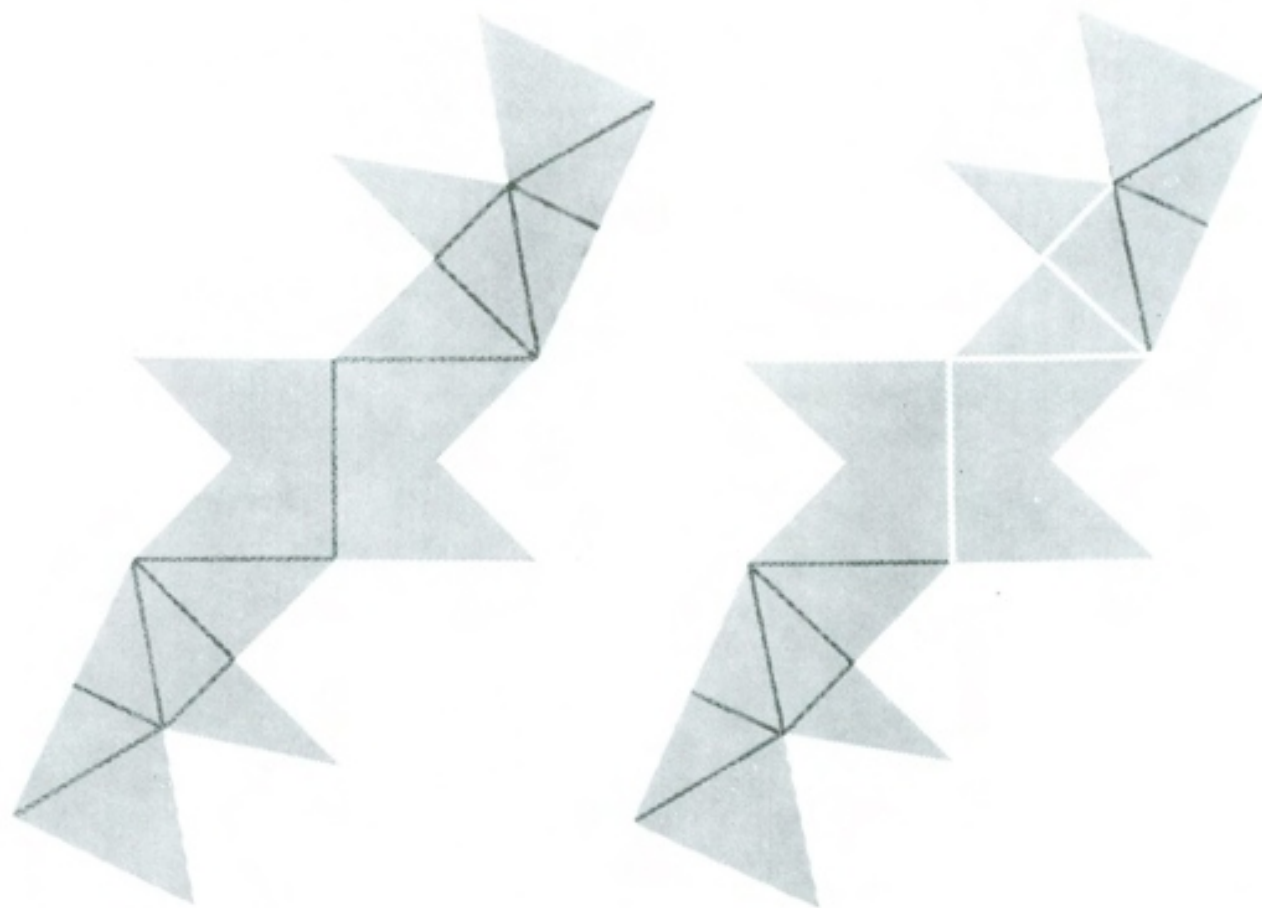
Quaderni di design

# MODELLI DI GEOMETRIA ROTATORIA

I moduli complementari  
e le loro combinazioni

a cura di Giorgio Scarpa





## ROTAZIONE-PIEGATURA DEGLI SVILUPPI

I collegamenti degli sviluppi di superficie esterna coi piani interni dell'esaedro determinano, come abbiamo visto, nuove configurazioni, nuovi sviluppi, ripiegando i quali, e passando quindi dal piano allo spazio, si ottengono moduli tridimensionali. Il passaggio da due dimensioni a tre dipende:

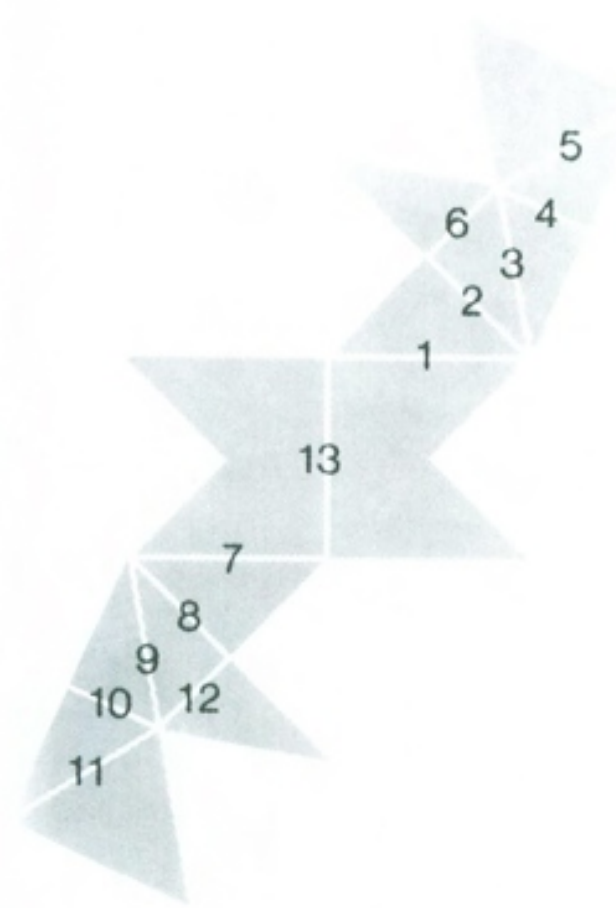
1. dal far assumere la funzione di assi di rotazione a linee che dimensionano le superfici degli sviluppi;

2. dall'individuare lungo queste configurazioni lineari, sequenze di piegatura costituenti determinati percorsi;

3. dalla scelta dei percorsi più logici ed economici;

4. dal ruotare (piegare) secondo determinati angoli, parti del modello intorno a queste linee (assi);

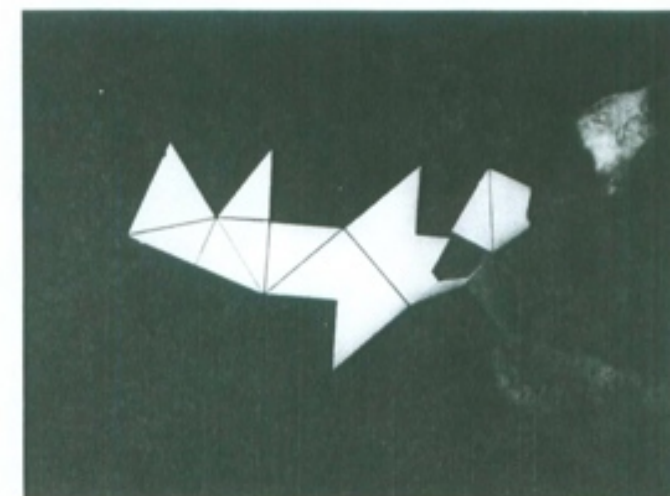
5. dal regolare numero e tipo di operazioni in riferimento a schemi di organizzazione formale.

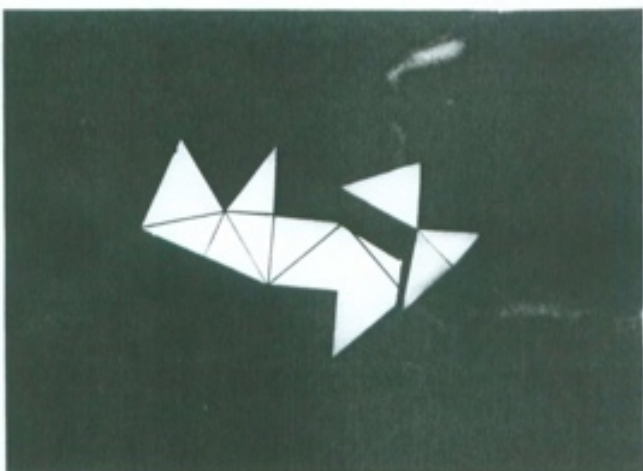


Esempi:  
ordine di piegatura indicato sulle linee interne dai numeri 1-13, relativo alla definizione del modulo;



cella cubica a cui riferire le sequenze di piegatura del modello.





Il percorso lineare intorno al quale ruotare i piani del modello è il seguente:



1. spigolo del cubo



4. metà asse interno



2. metà diagonale di una faccia



5. metà diagonale interna



3. metà diagonale interna



6. metà asse interno



9. metà diagonale interna



7. spigolo



10. metà asse interno



8. metà diagonale di una faccia



11. metà diagonale interna







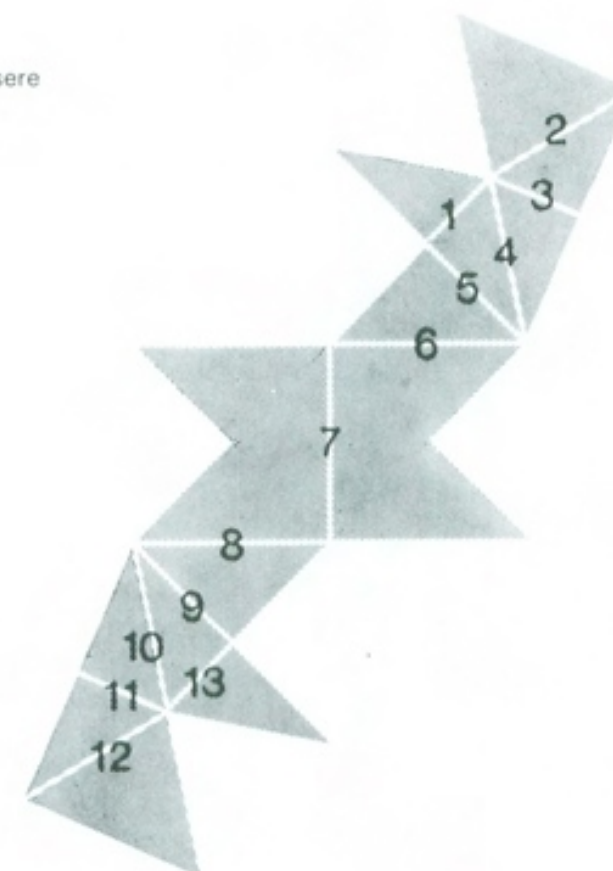
12. metà asse interno



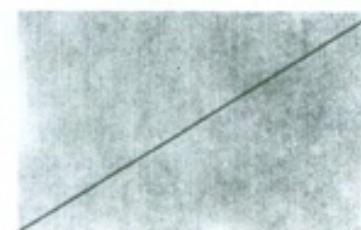
13. spigolo  
Le rotazioni sono di 90°.



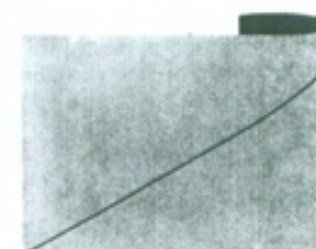
Uno stesso sviluppo può essere  
variamente ripiegato.



A

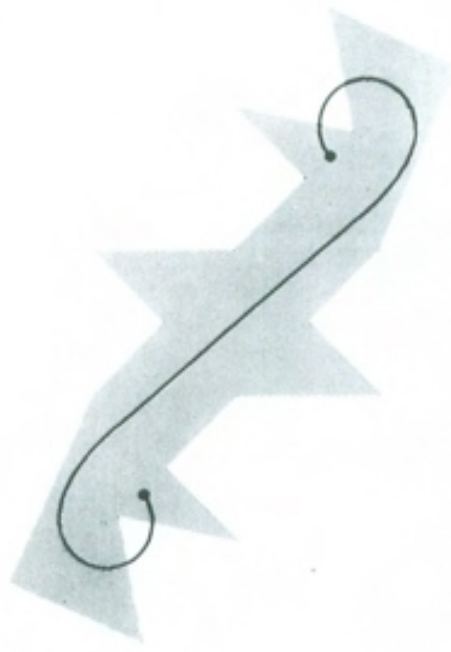
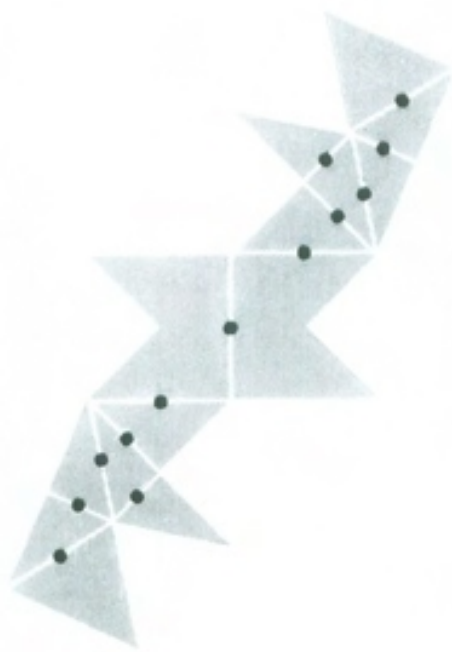


B

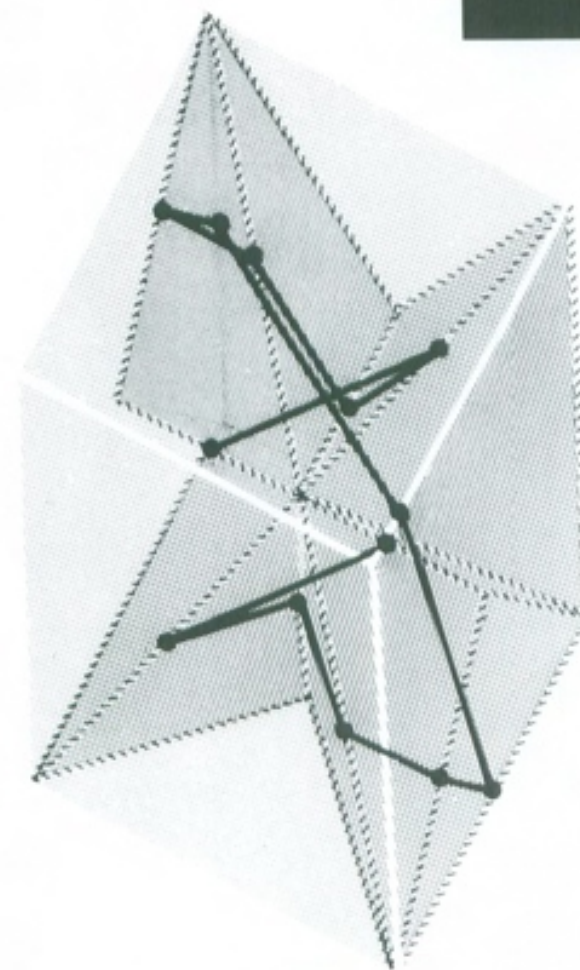
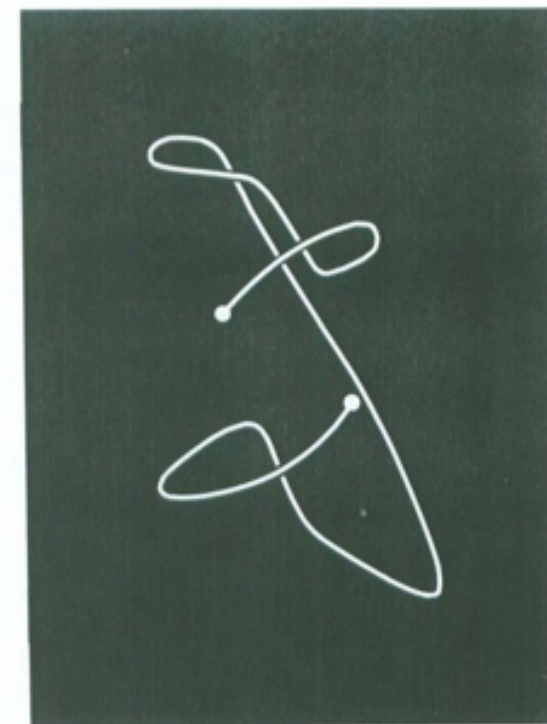
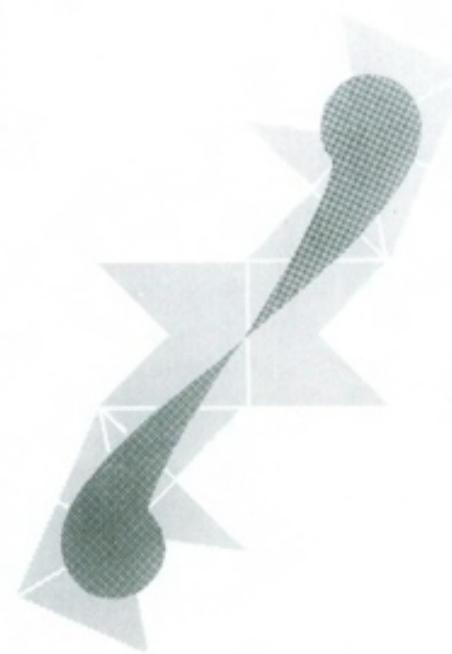


Che cos'è un'elica? è la curva spontanea  
disegnata nell'aria dai semi del tiglio quando  
si staccano dalla pianta;  
o dalla terra, che ruotando nello spazio intorno  
al Sole si sposta sull'asse di avanzamento del  
Sole verso la stella Vega;  
è per il pittore Paul Klee "...la più pura forma  
di movimento pensabile".  
In geometria, è nella sua forma più semplice,  
lo sviluppo cilindrico della diagonale  
di un rettangolo.

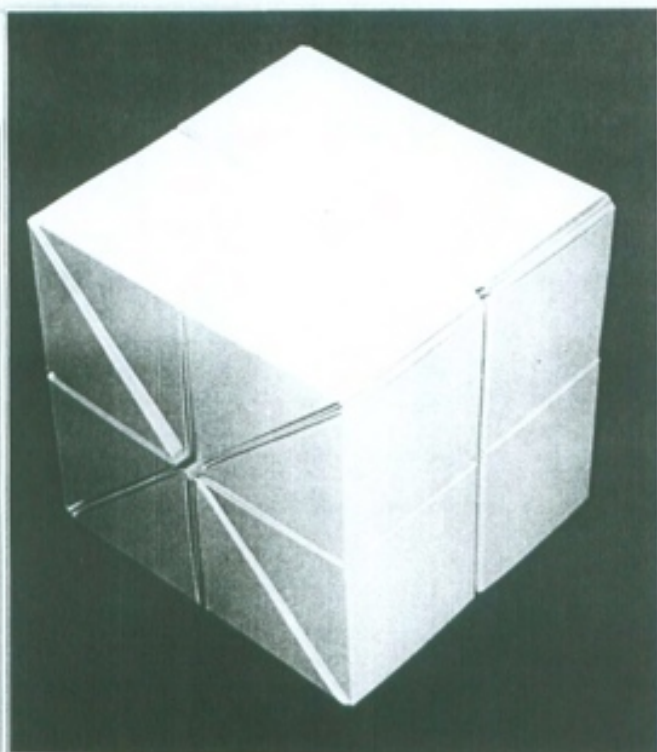




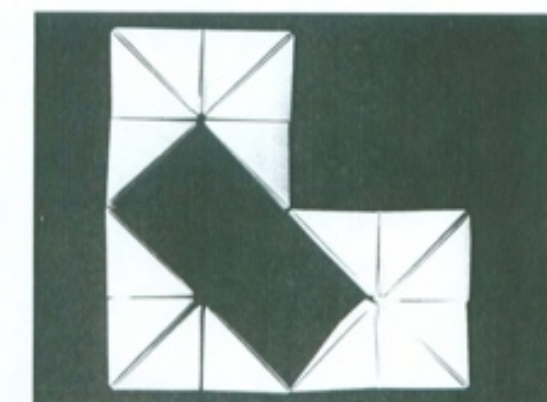
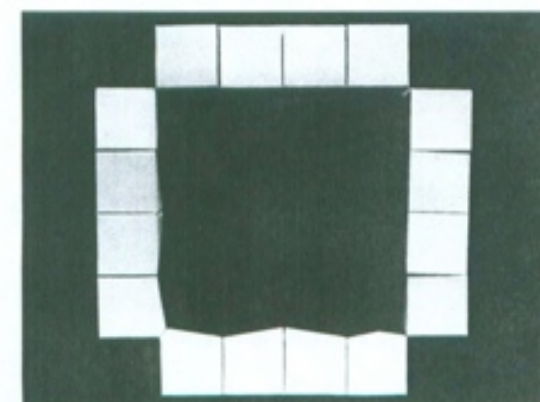
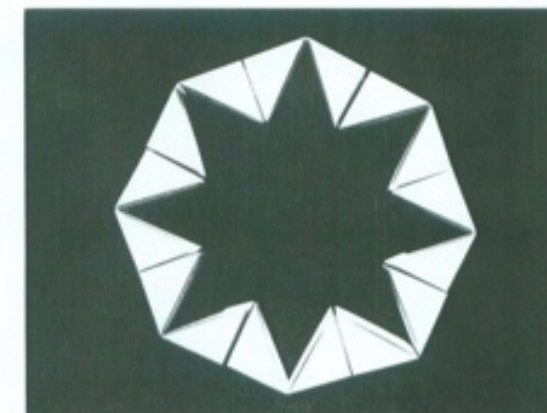
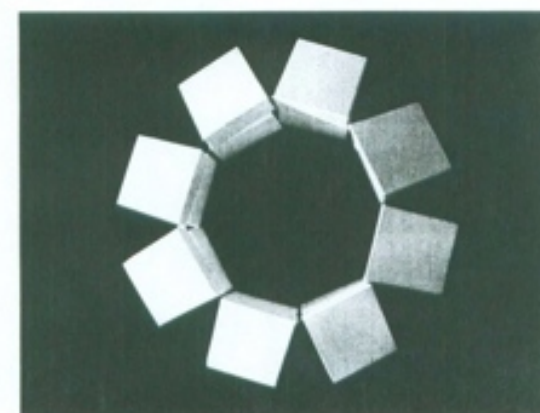
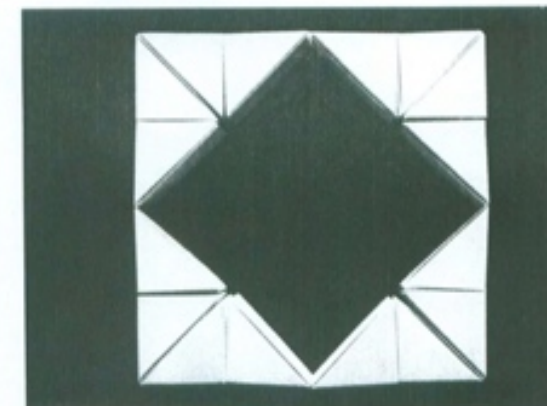
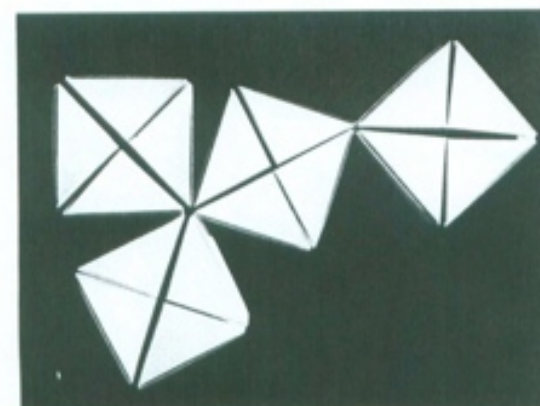
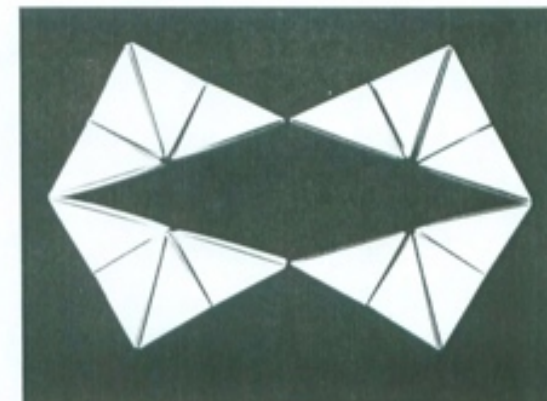
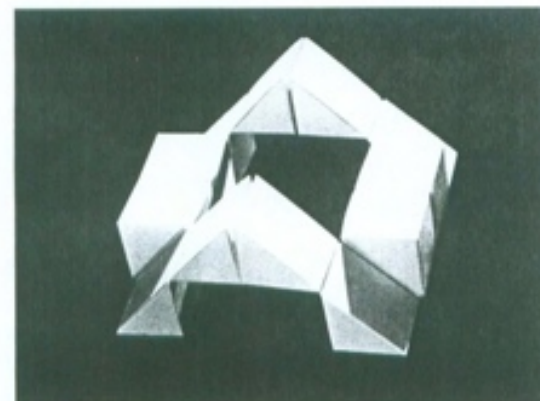
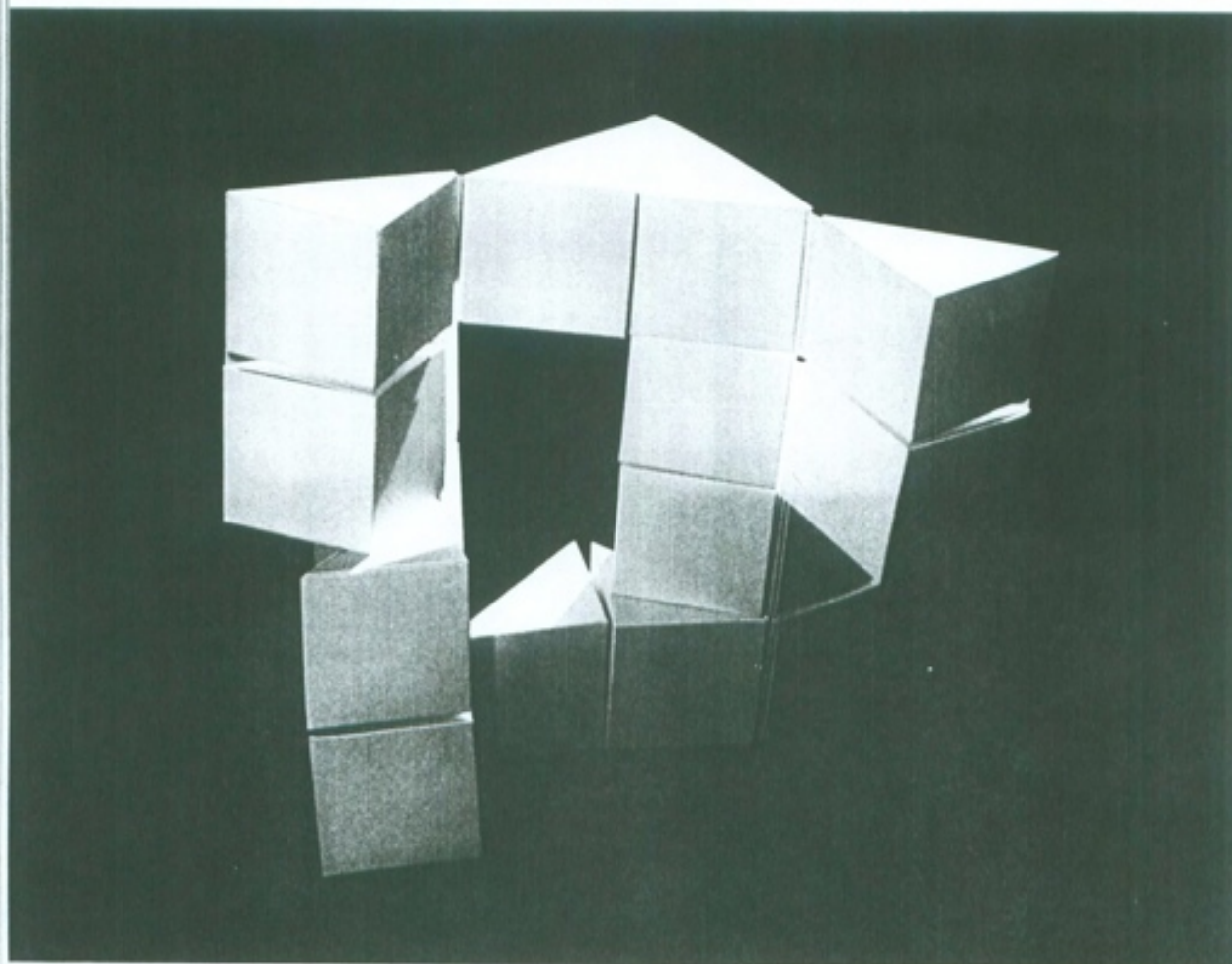
Consideriamo i piani articolati in due raggruppamenti (1-7 e 7-13, v. pagine precedenti) intorno al centro di rotazione 7; la loro forma complessiva è simile ad una esse che risulta più visibile se con una linea curva raccordiamo tra loro i punti da 1 a 13, o disegniamo due regioni che delimitano il tracciato puntiforme, accentuando l'andamento ciclico a due bracci dello sviluppo. La composizione dei movimenti di piegatura con cui portiamo nello spazio i piani, ruotandoli intorno agli assi 1-13, dà come risultante una traiettoria a forma di elica. Con questa mappa spaziale che unifica la successione dei movimenti, definiamo lo sviluppo in terza dimensione. La rappresentazione di mappe dei movimenti di ripiegamento deve avere come fine il controllo dell'intero processo, in vista della sua semplificazione.



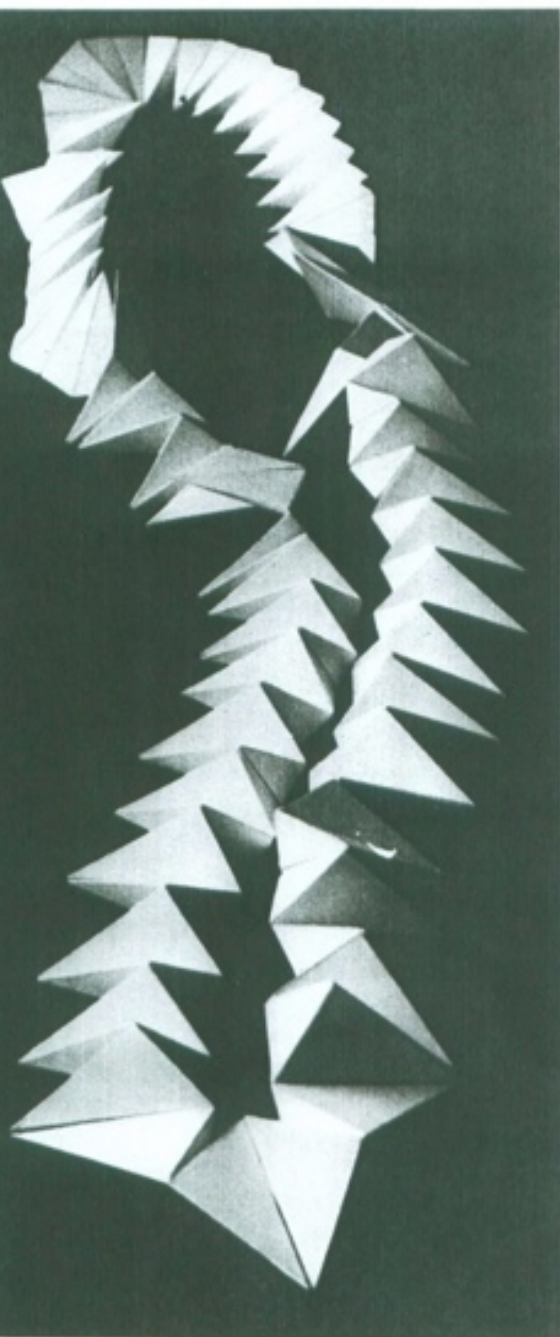




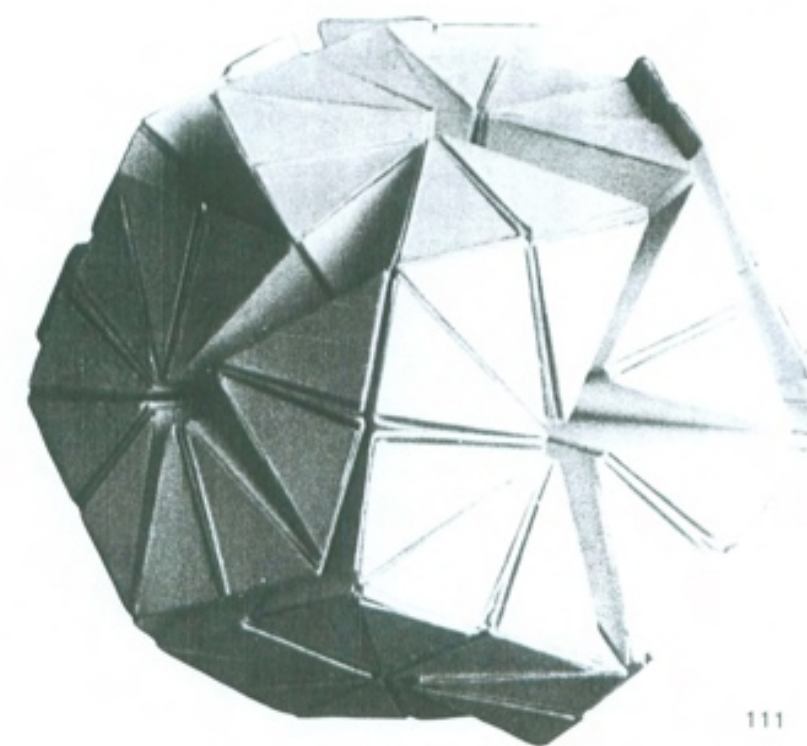
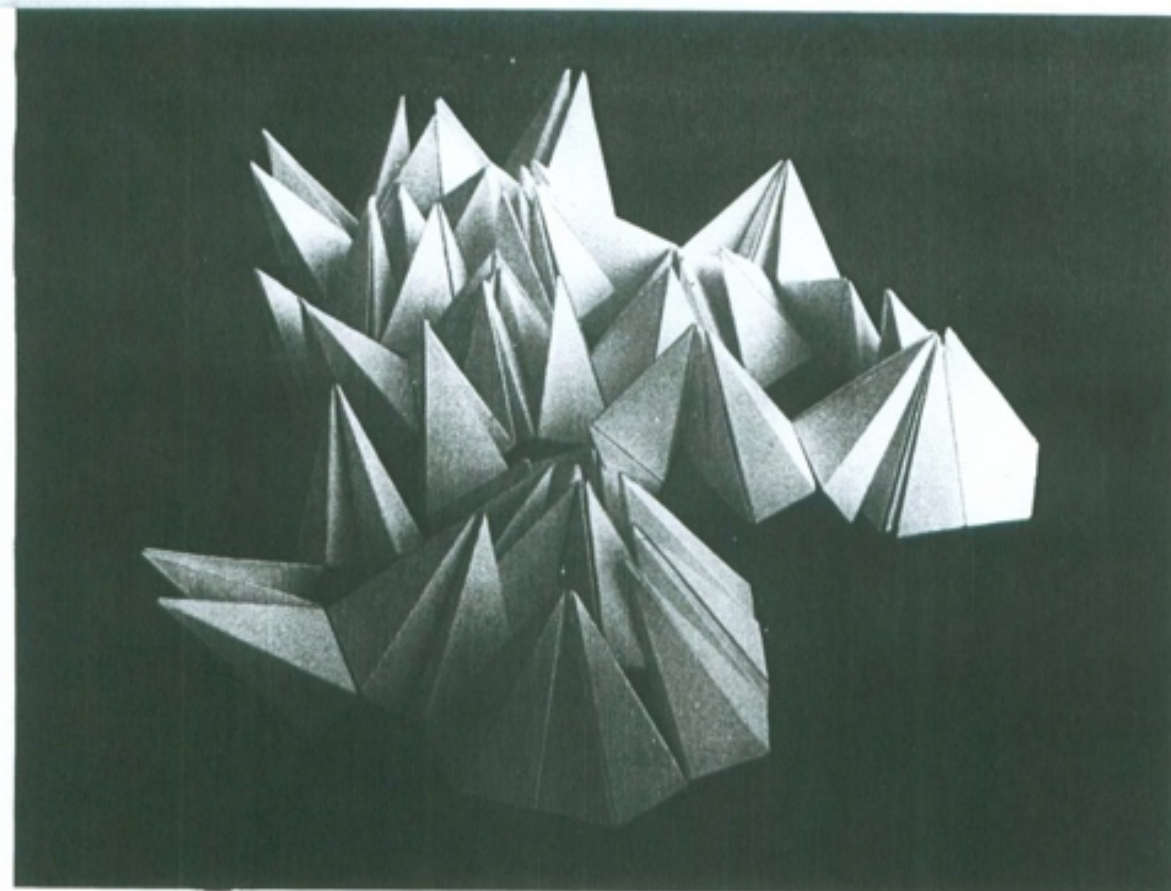
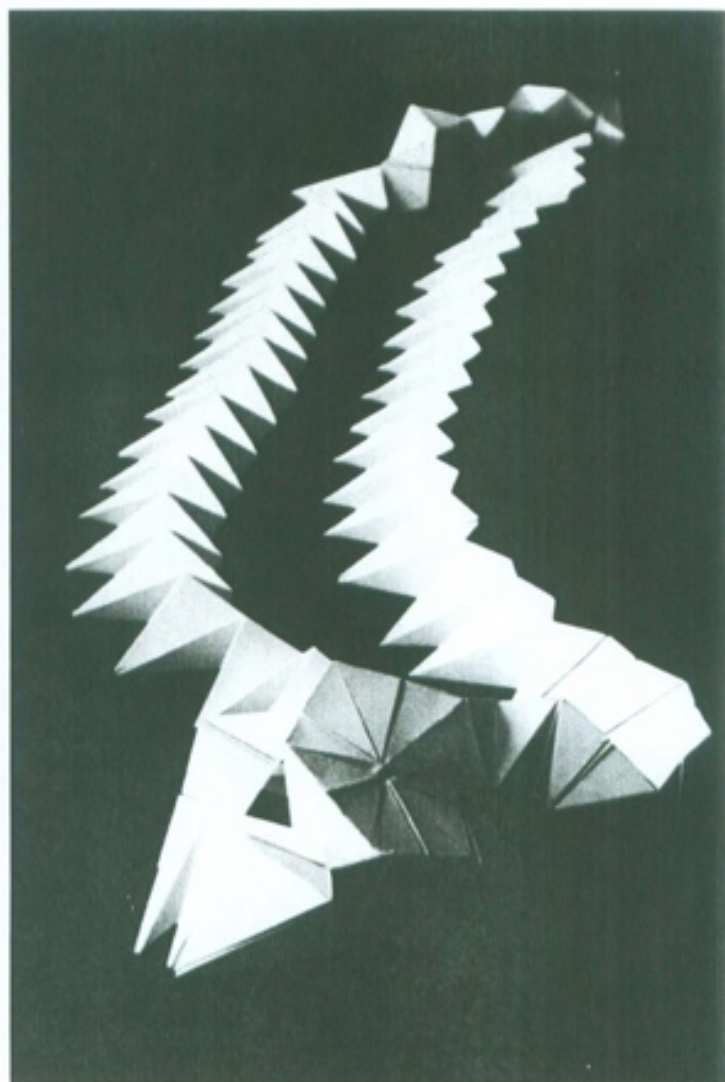
Rotazioni di catene esaedriche.







110



111







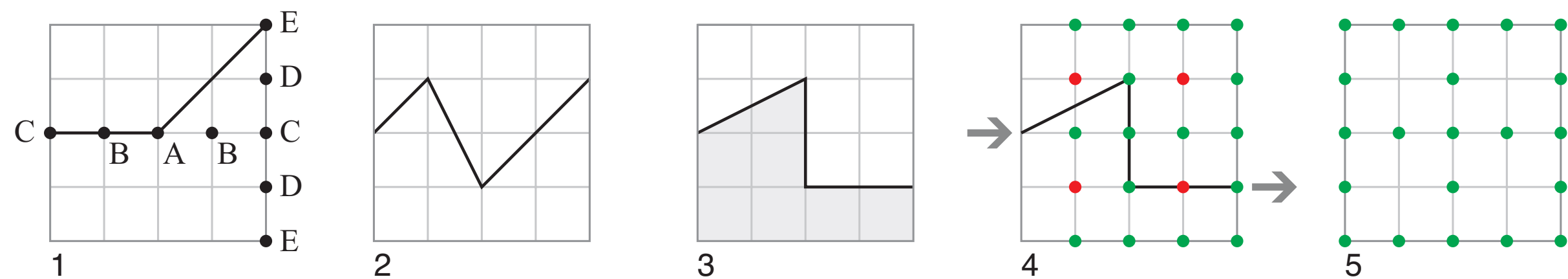






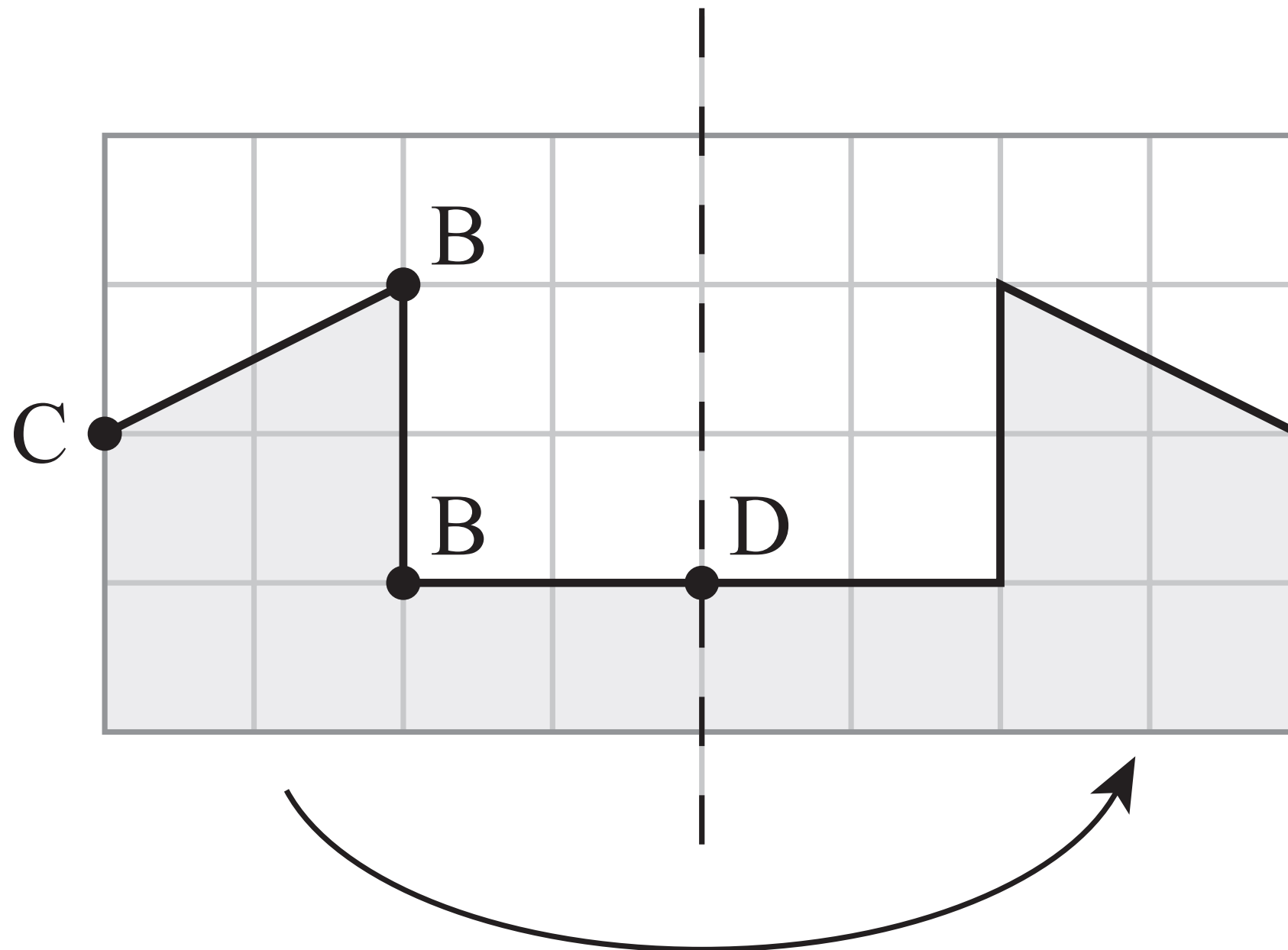


# TWIN SECTION



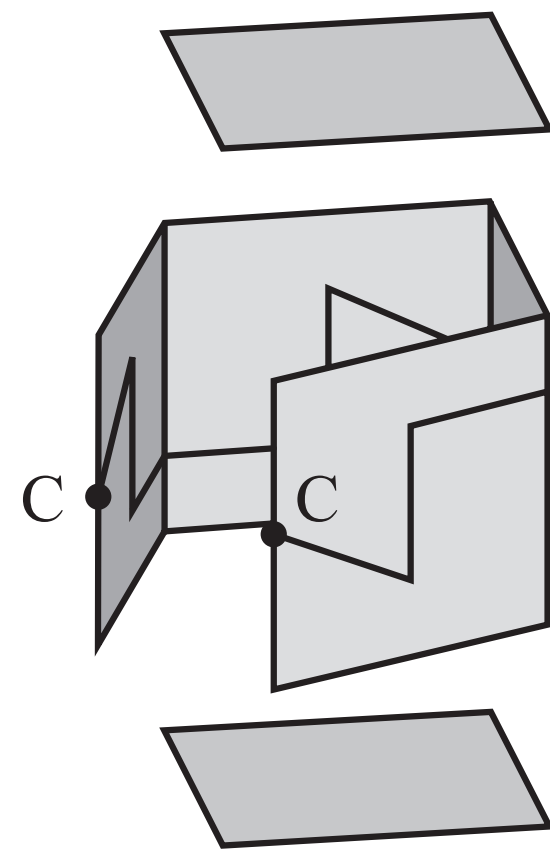
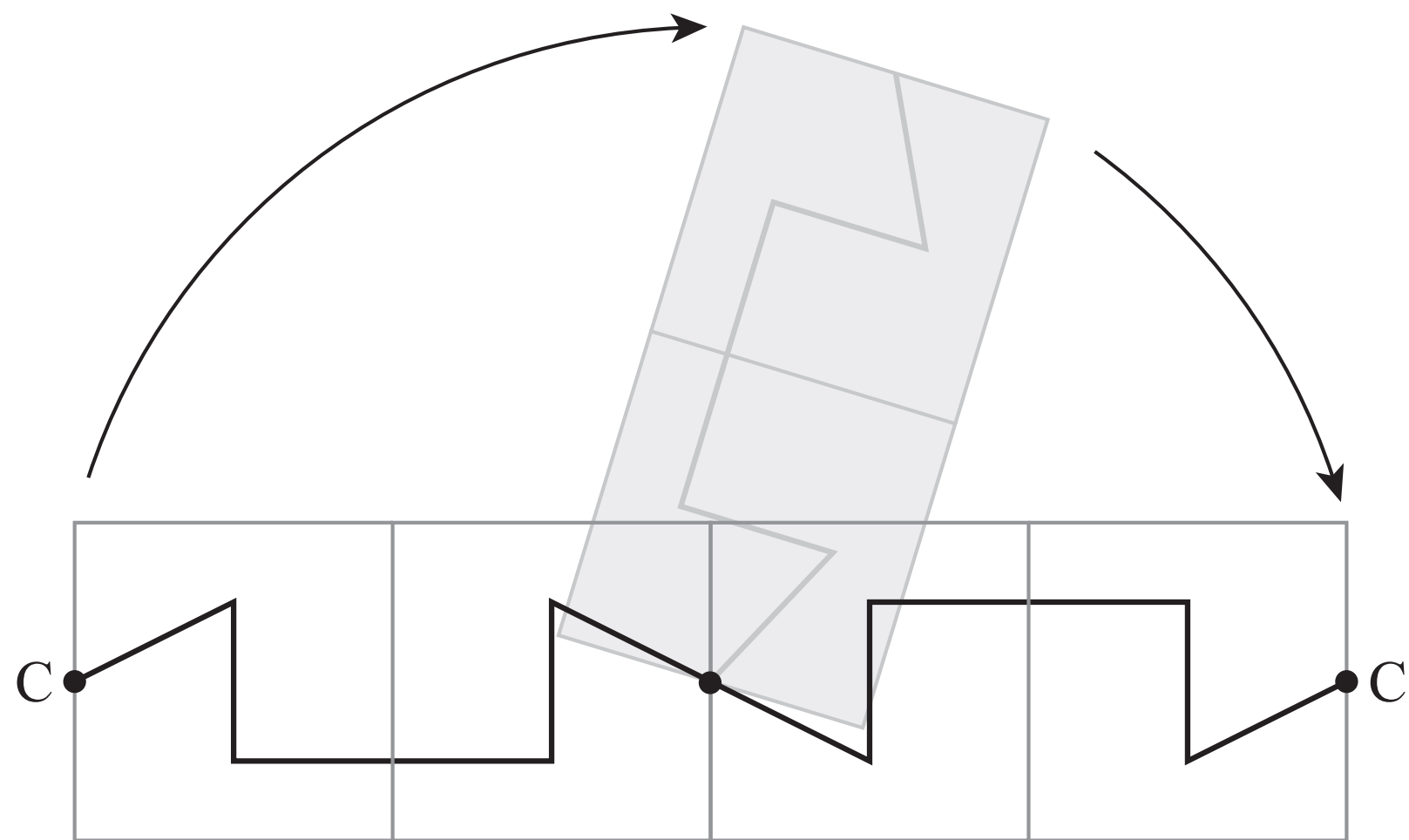
**Fig. 1**





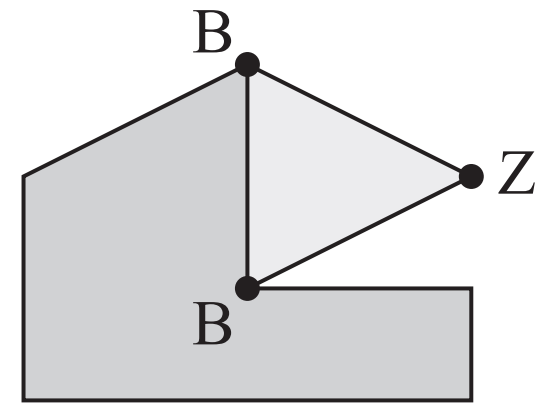
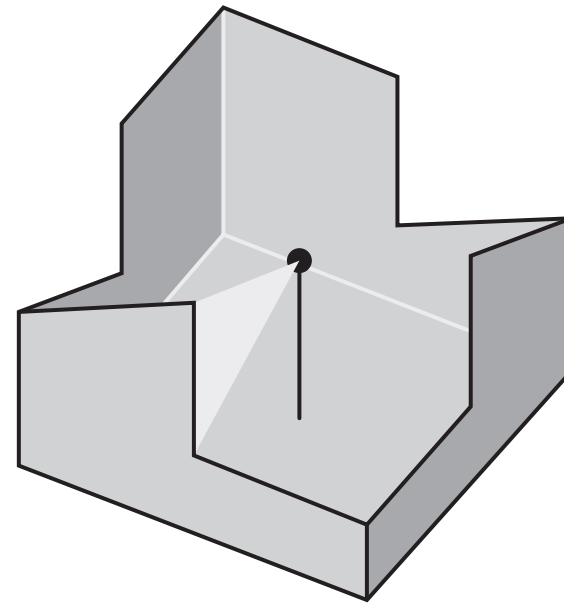
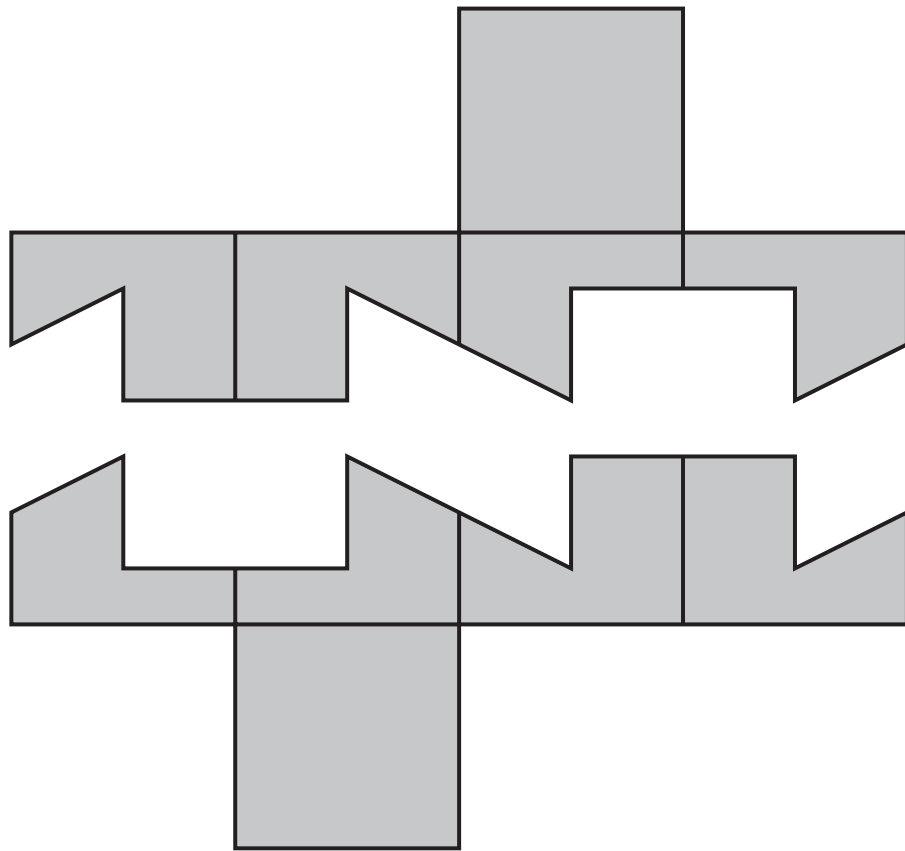
**Fig. 2**





**Fig. 3**



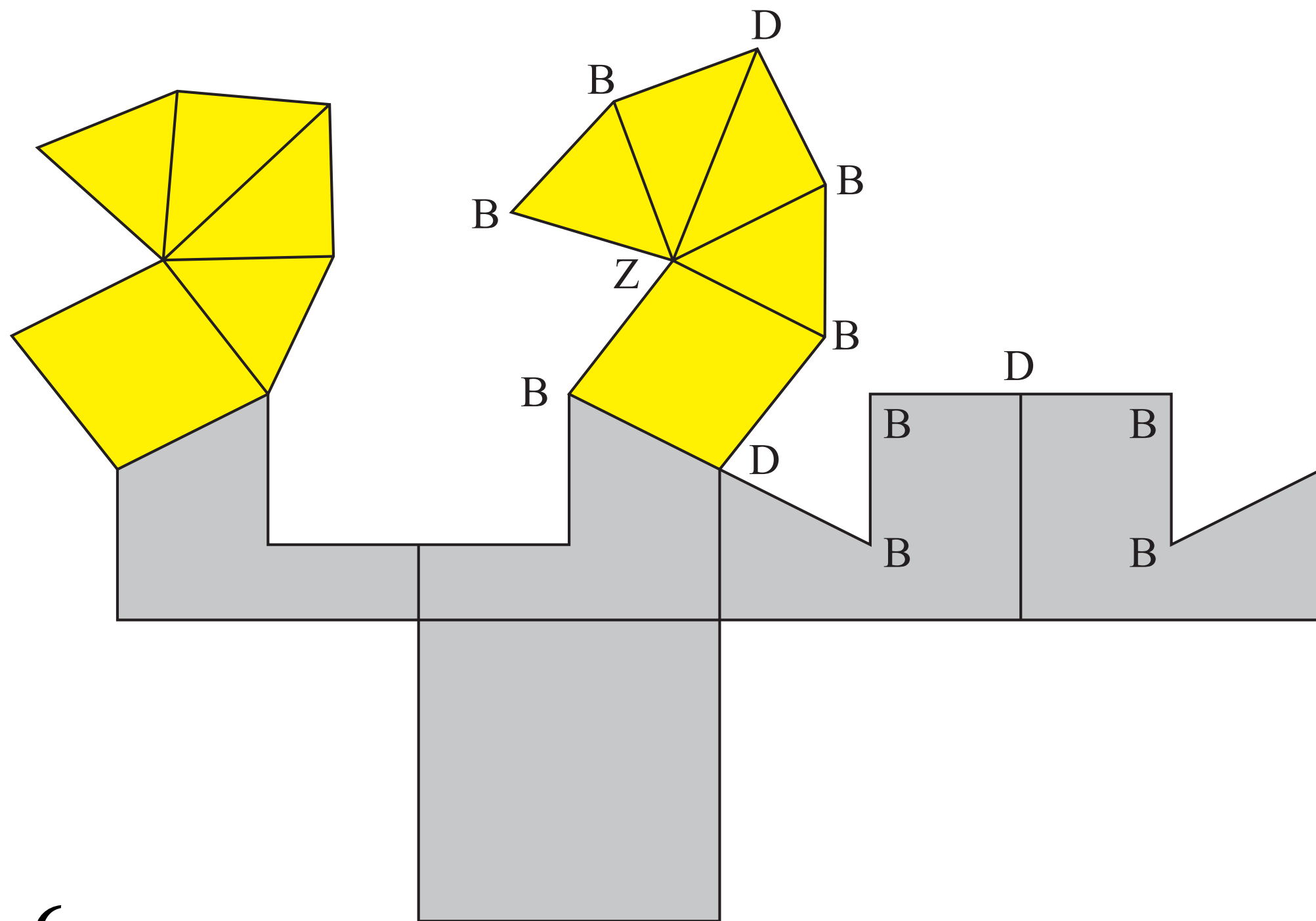


**Fig. 4**



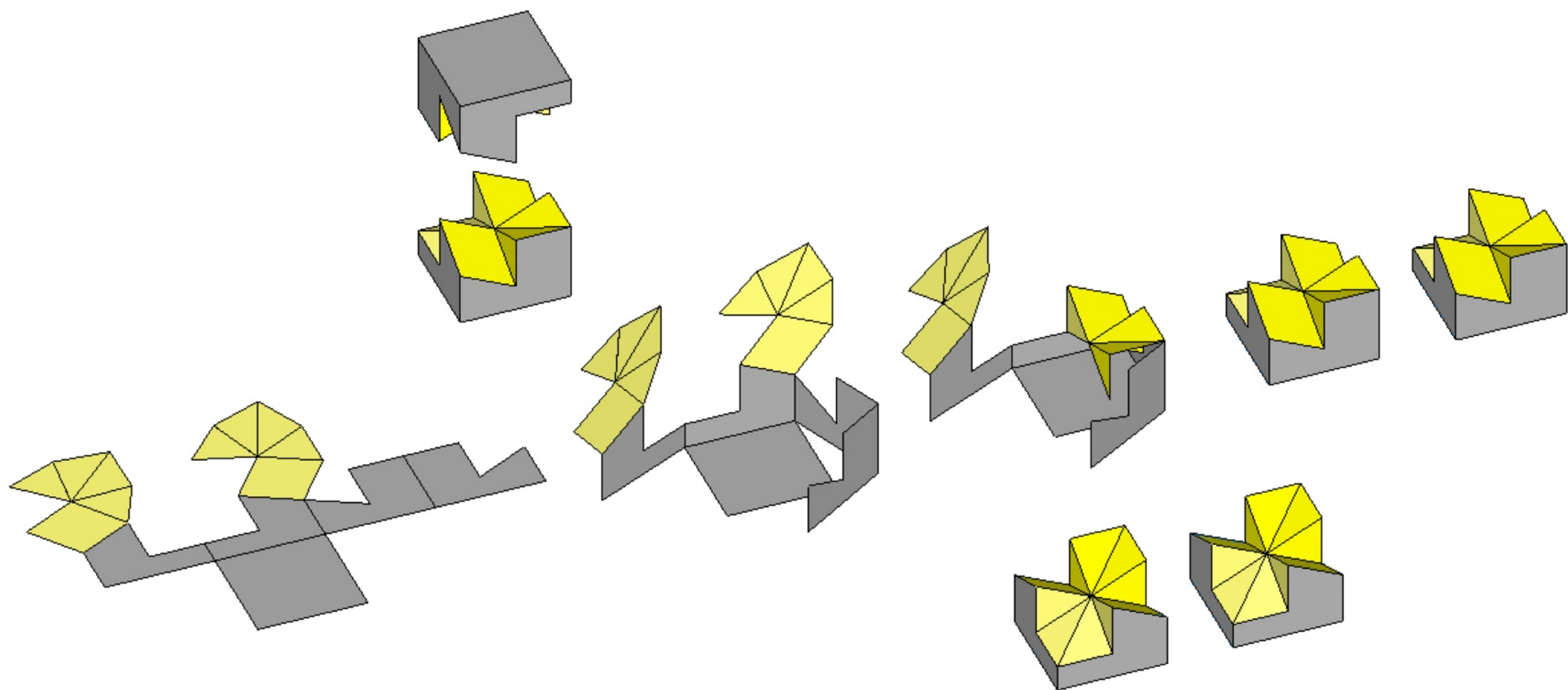






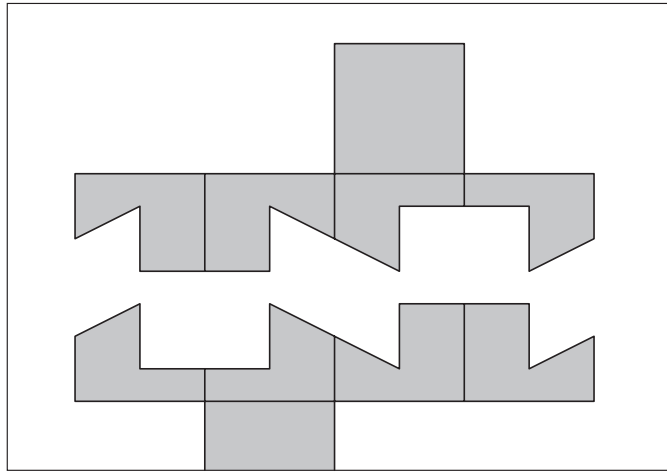
**Fig. 6**



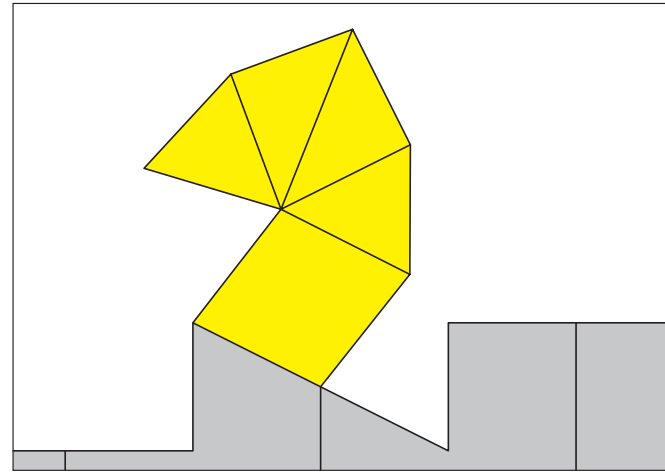


**Fig. 7**

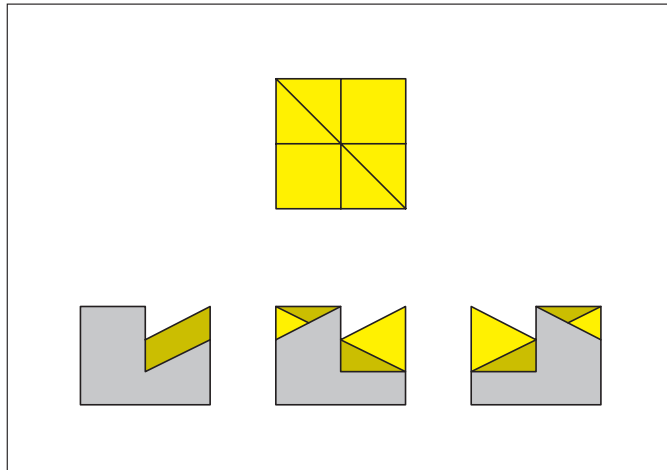




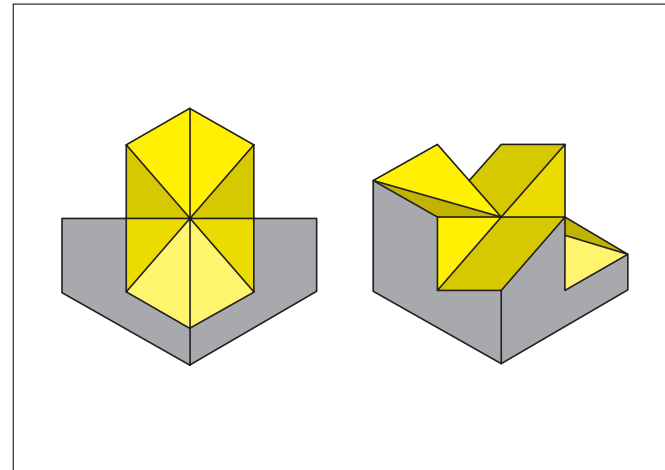
8



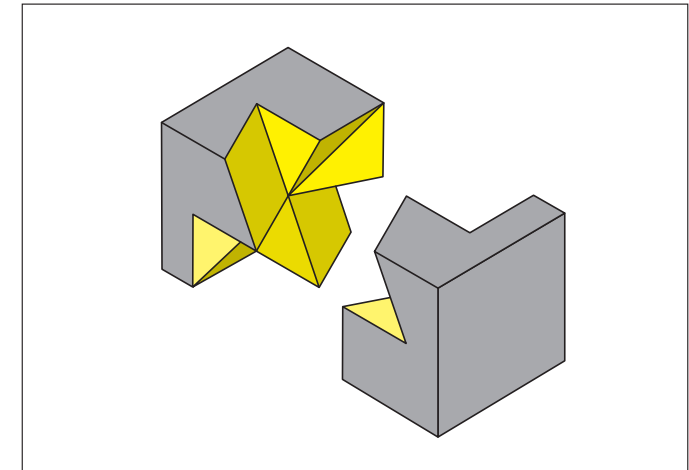
9



10



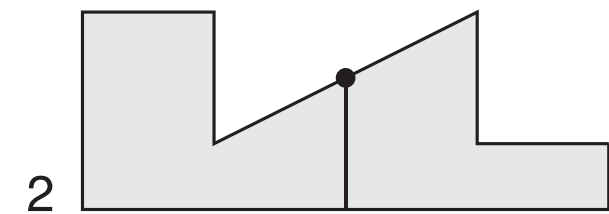
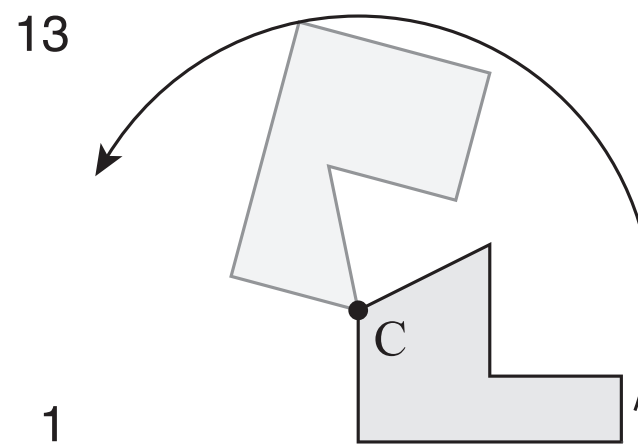
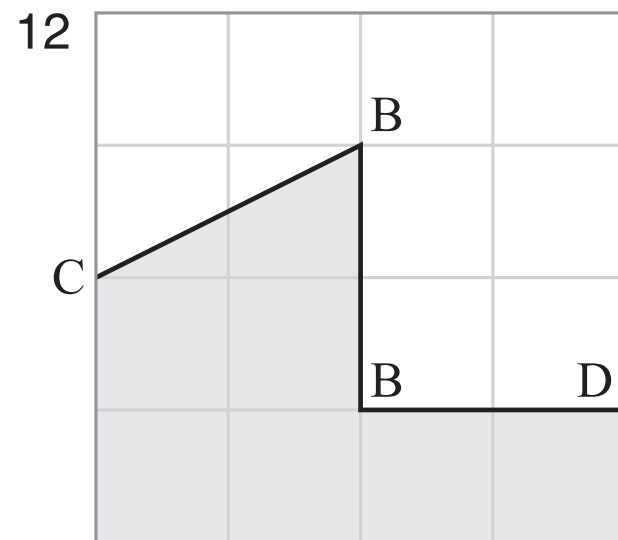
11A



11B

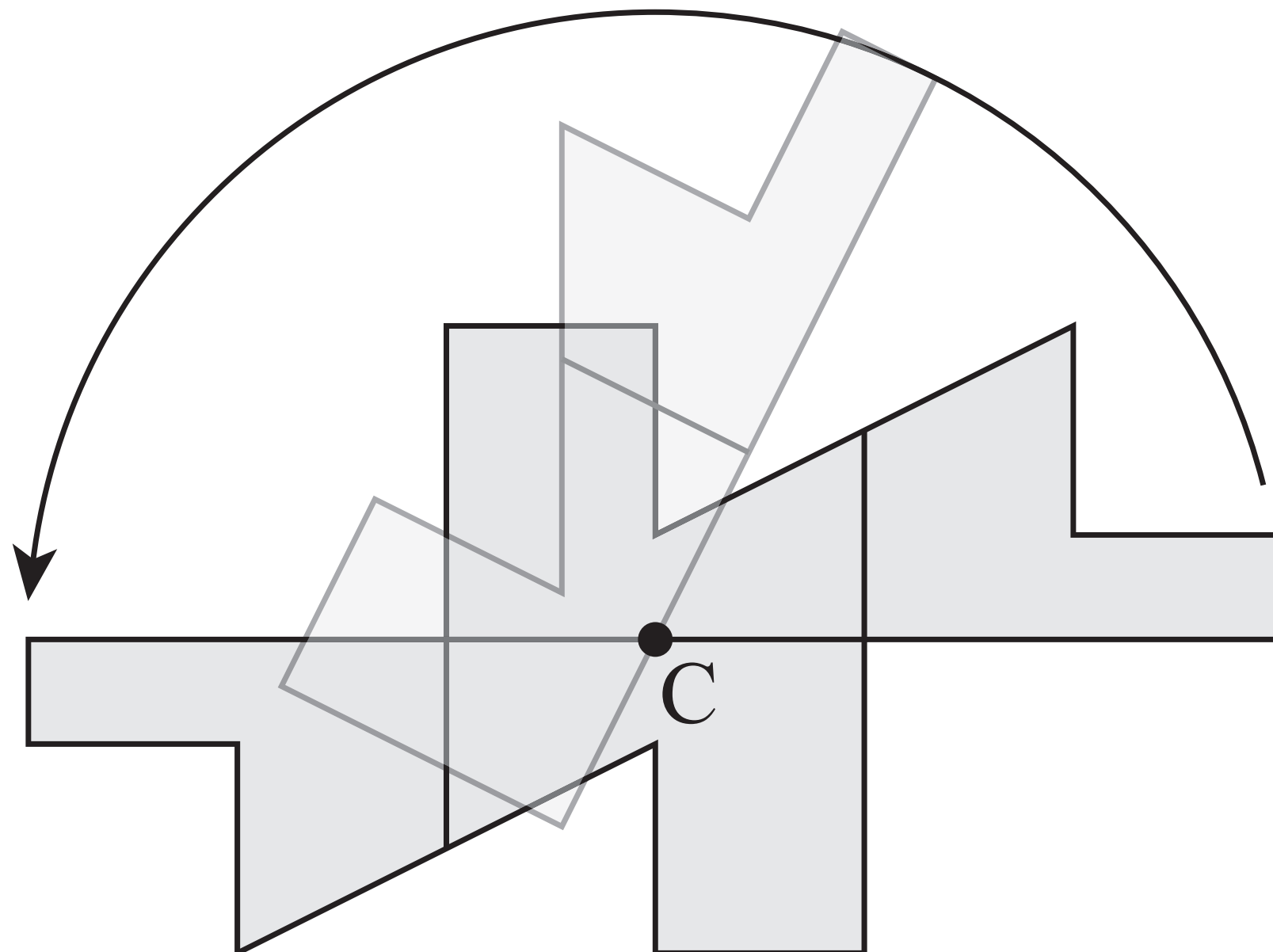
**Fig. 8-11**

# TRIPLET SECTION

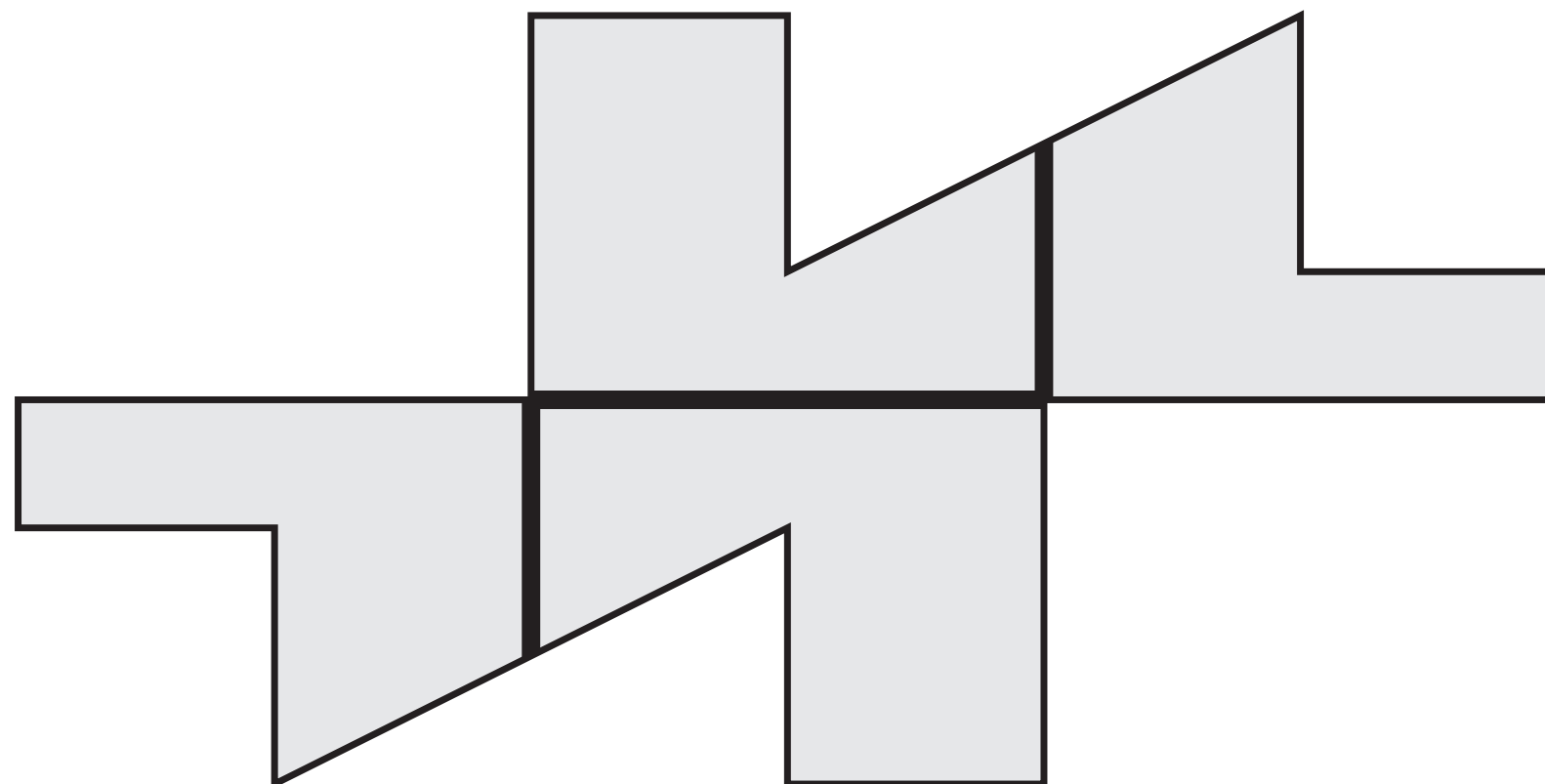


**Fig. 12-13**



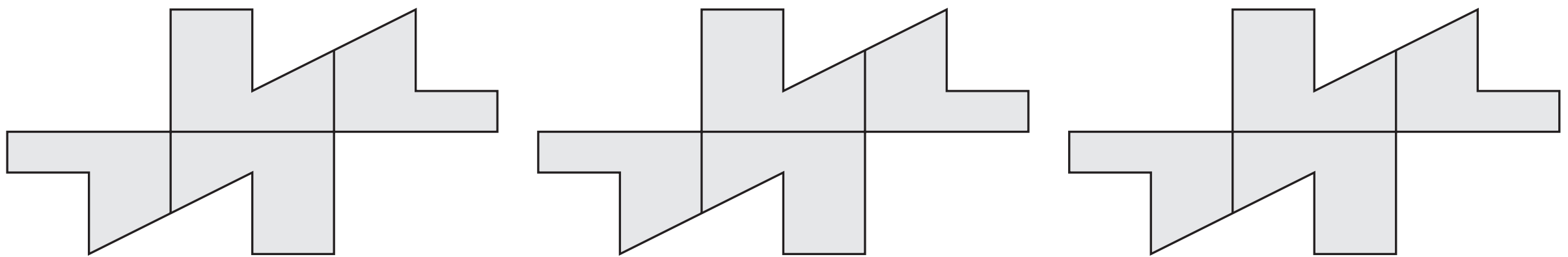


**Fig. 14**

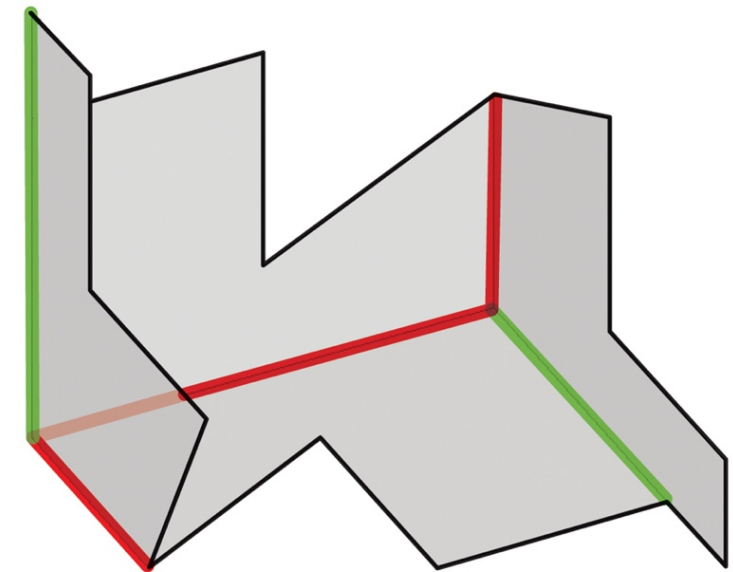
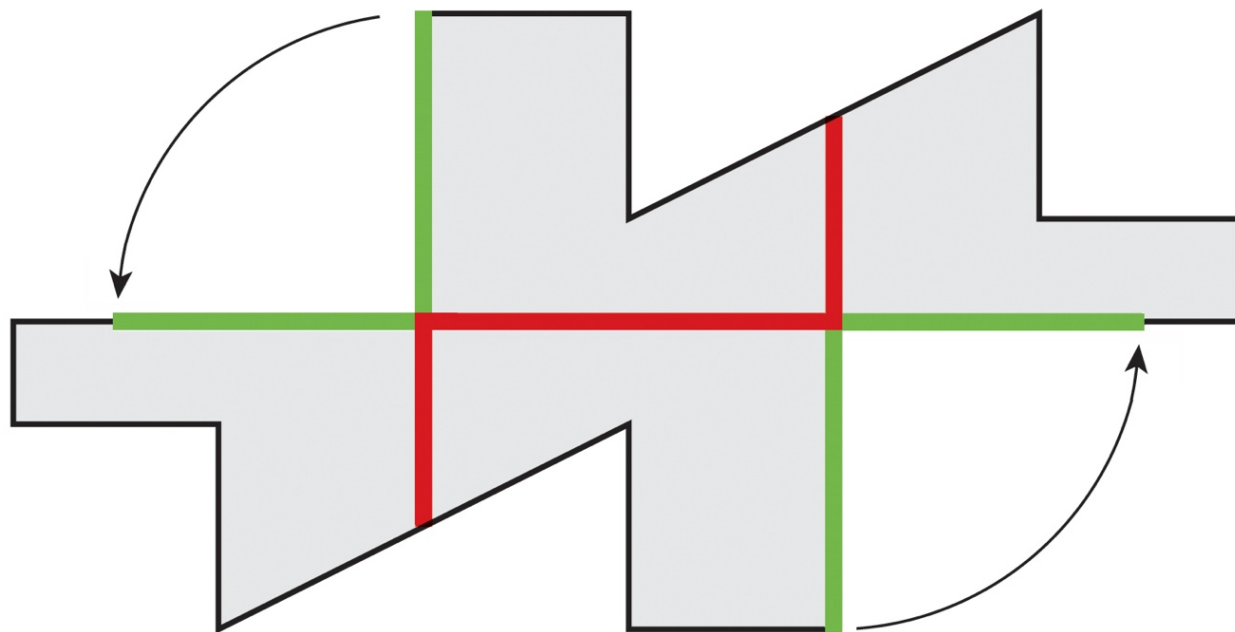


***Fig. 15***



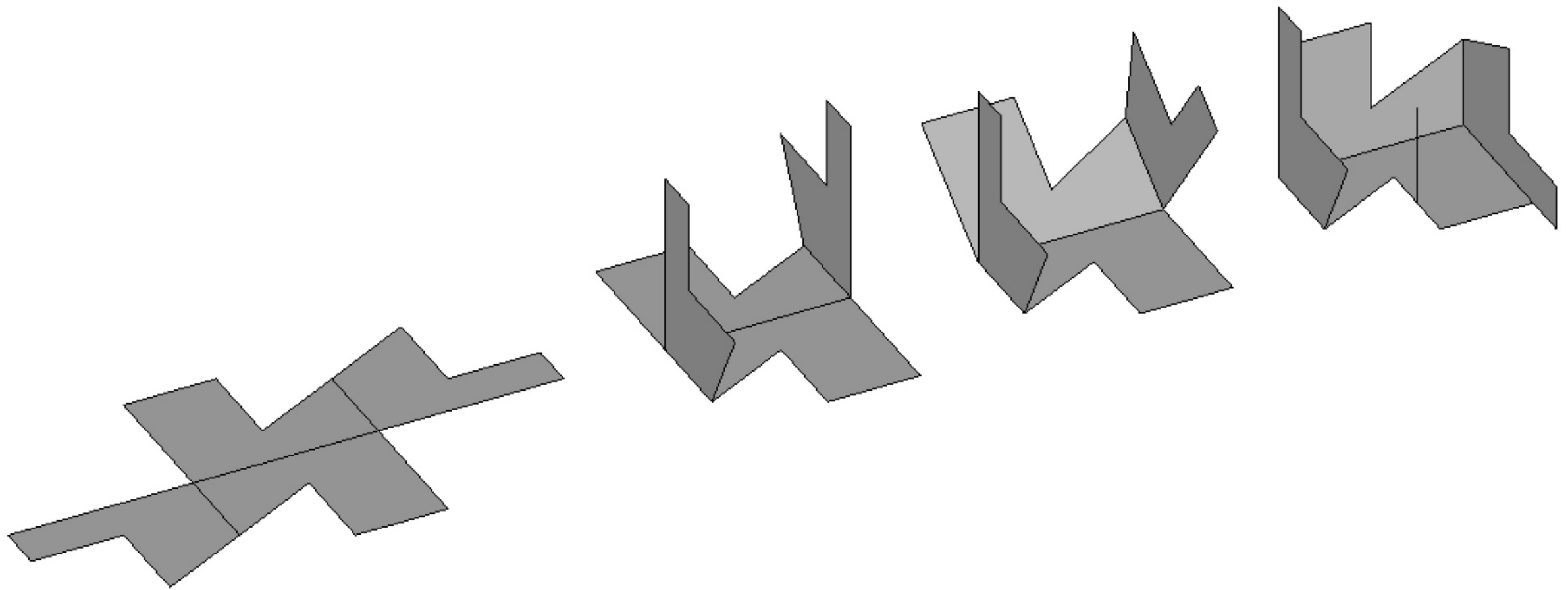


***Fig. 16***

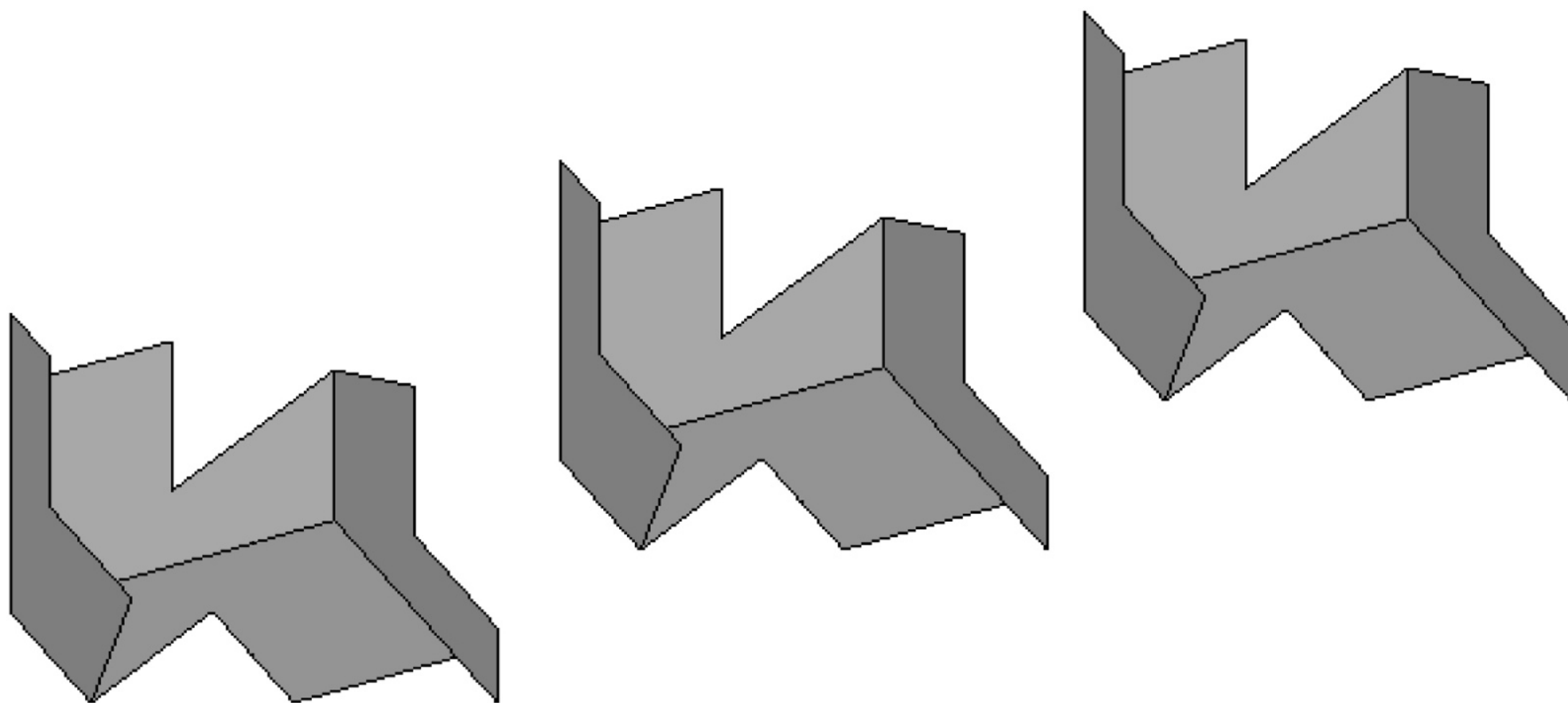


**Fig. 17**



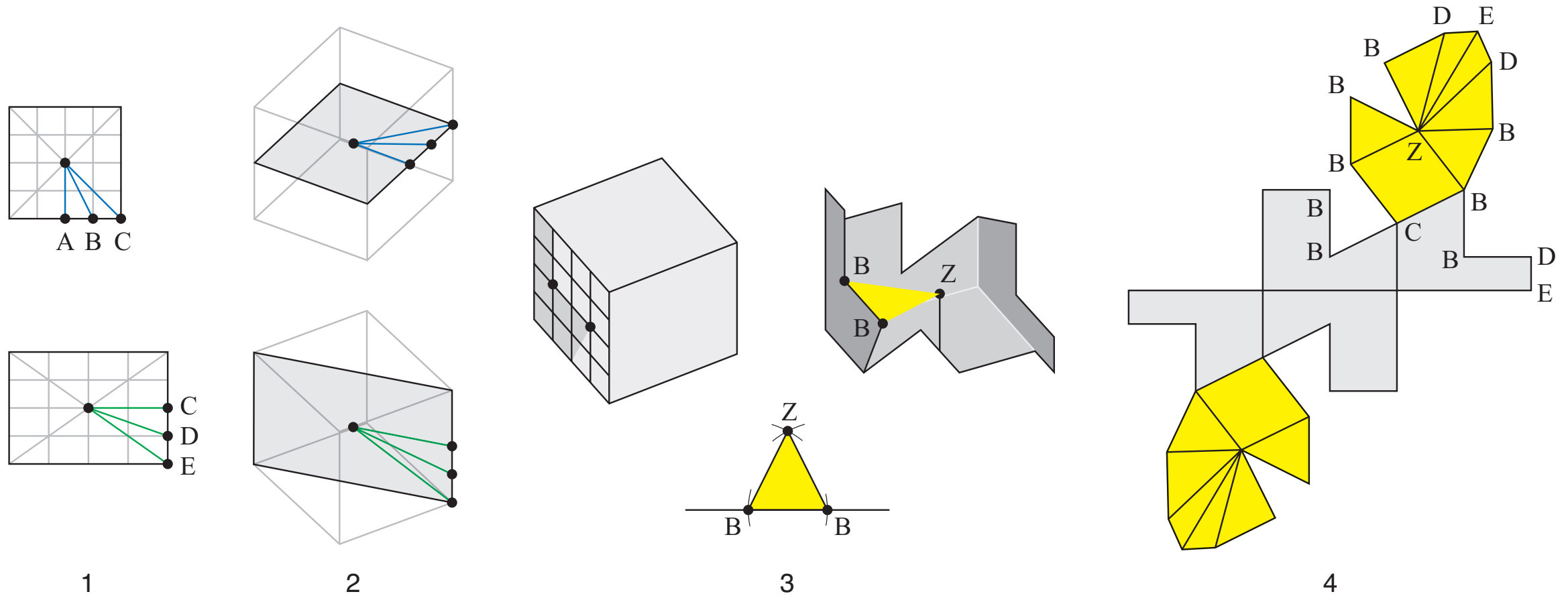


**Fig. 18**

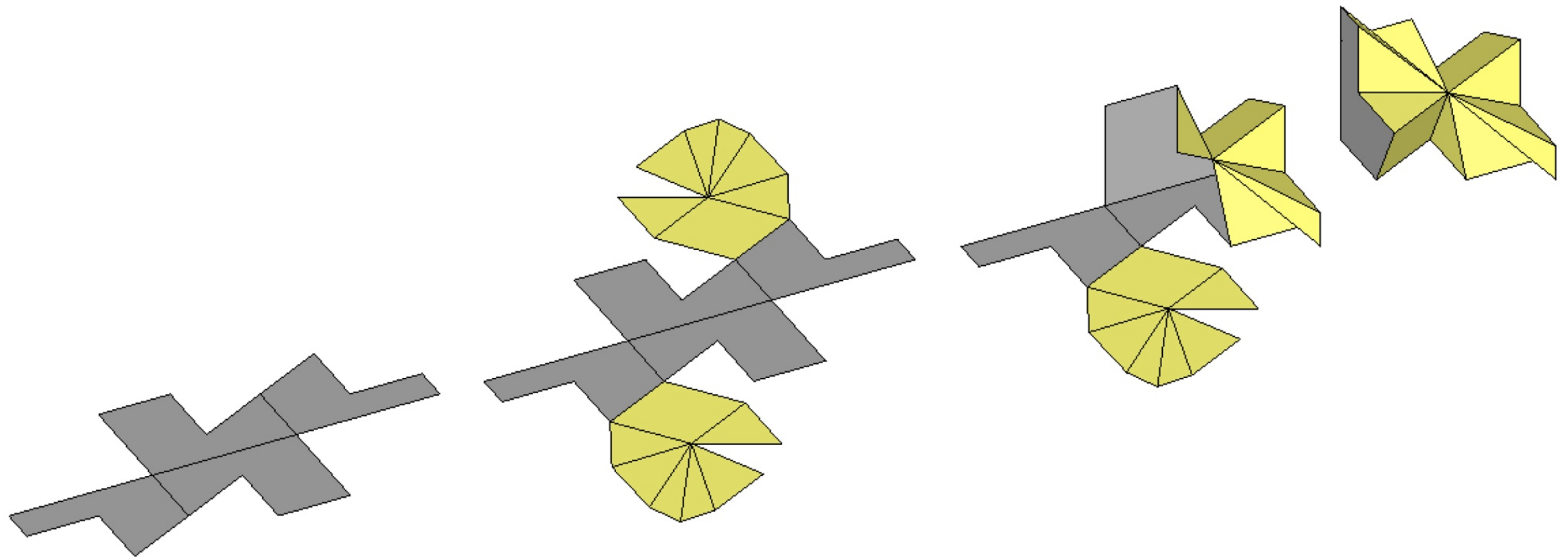


**Fig. 19**



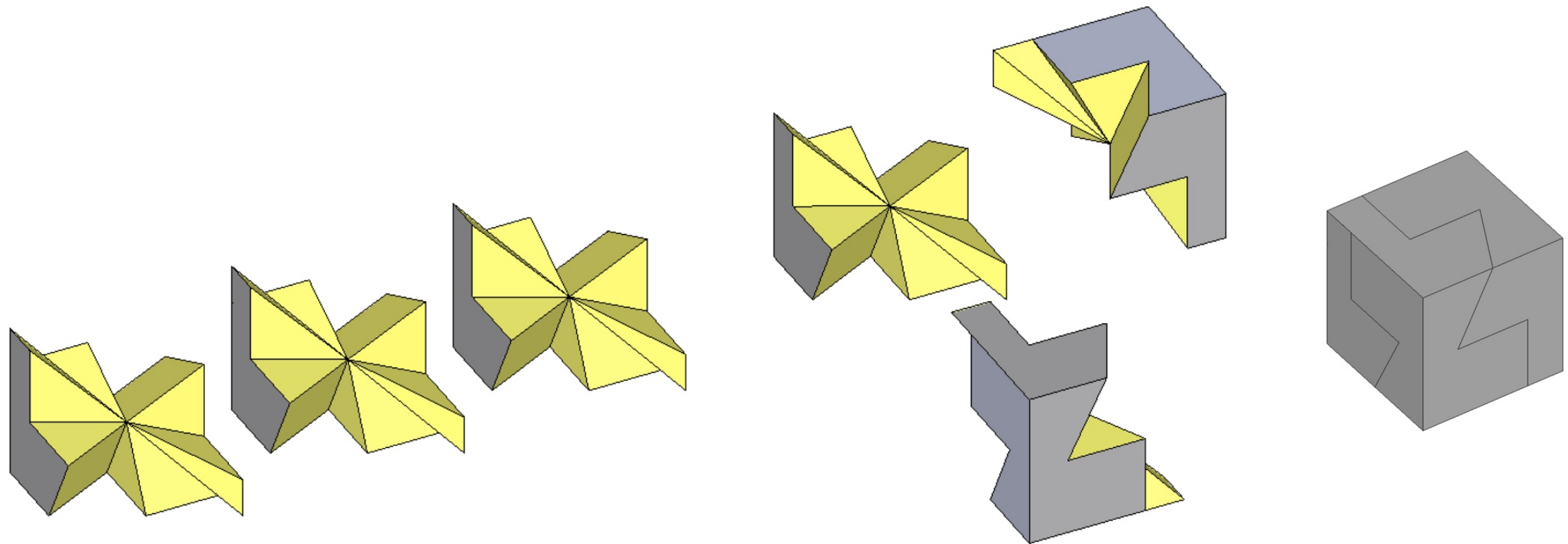


**Fig. 20**

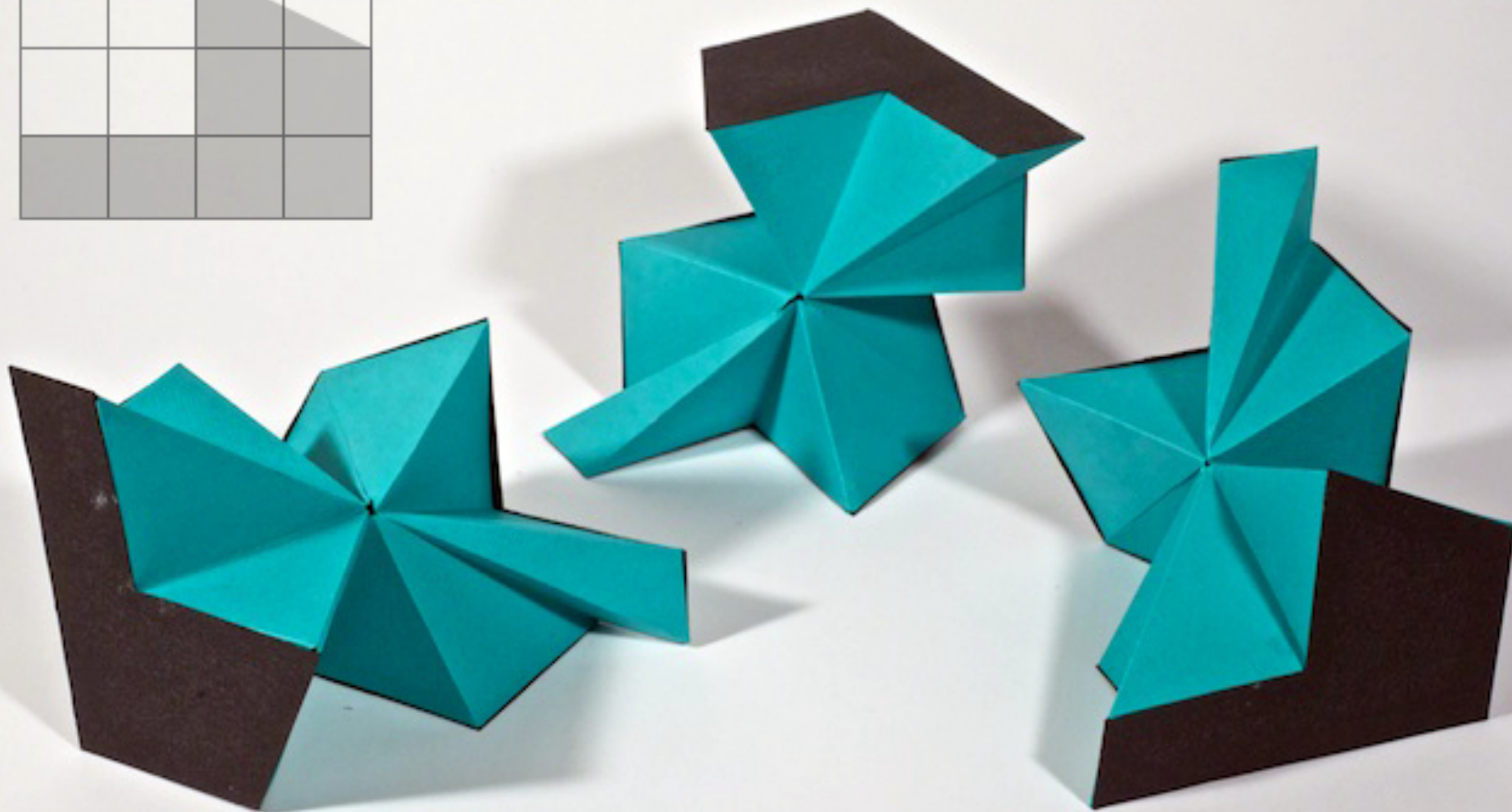
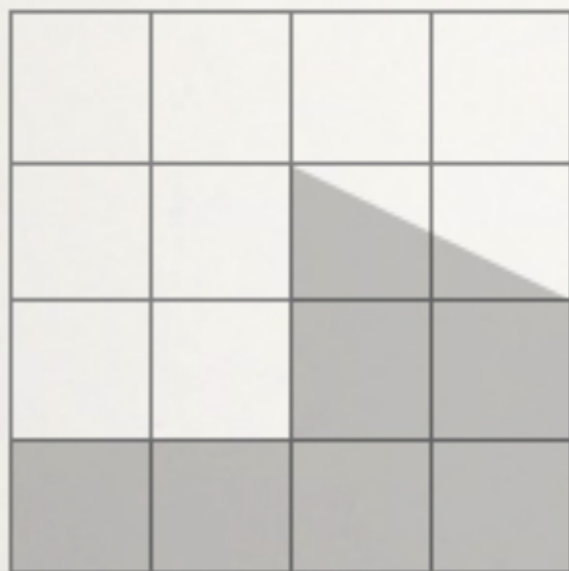


**Fig. 21**



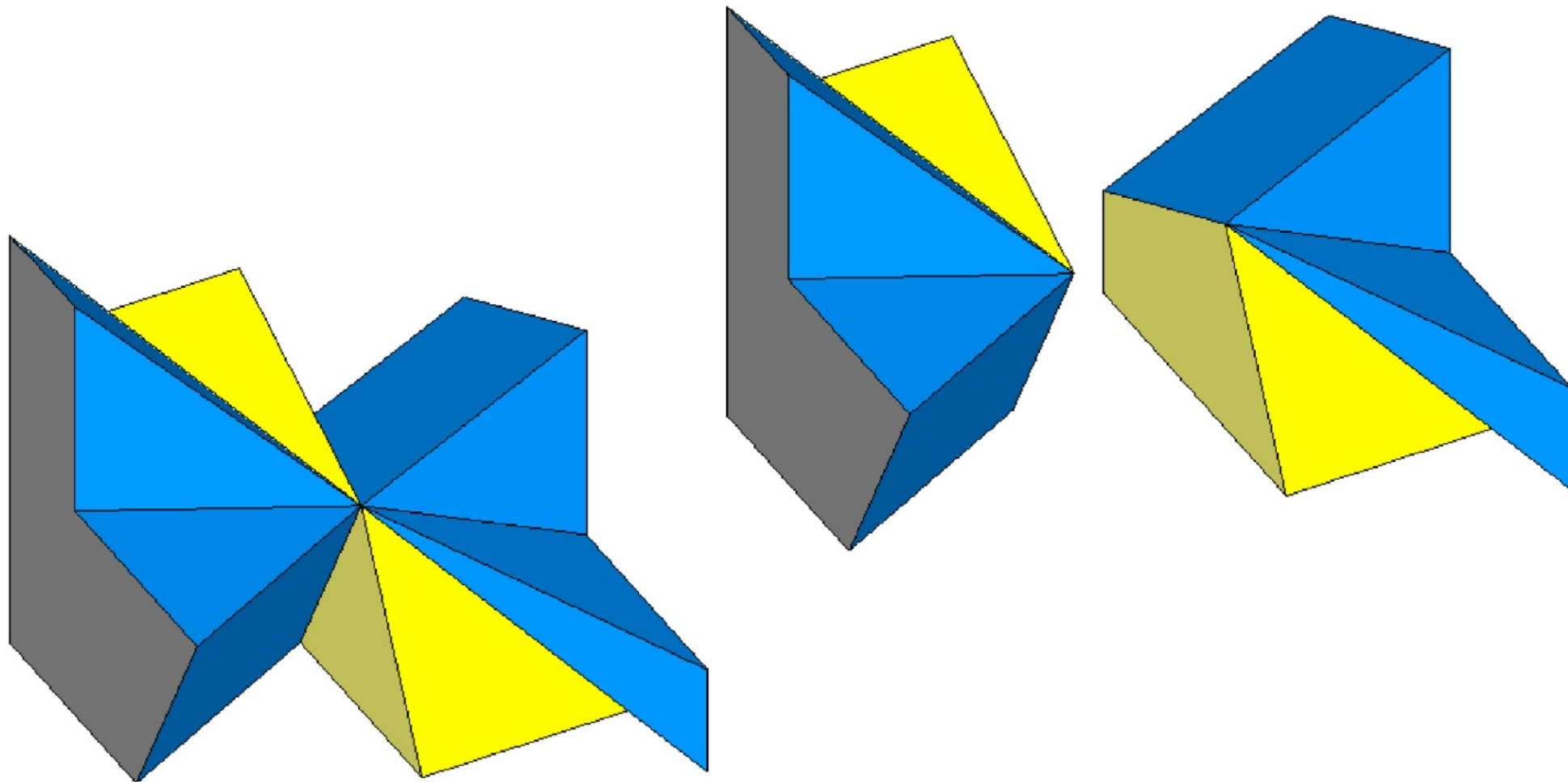


**Fig. 22**



**Fig. 23**

# HINGES AND ROTATIONS



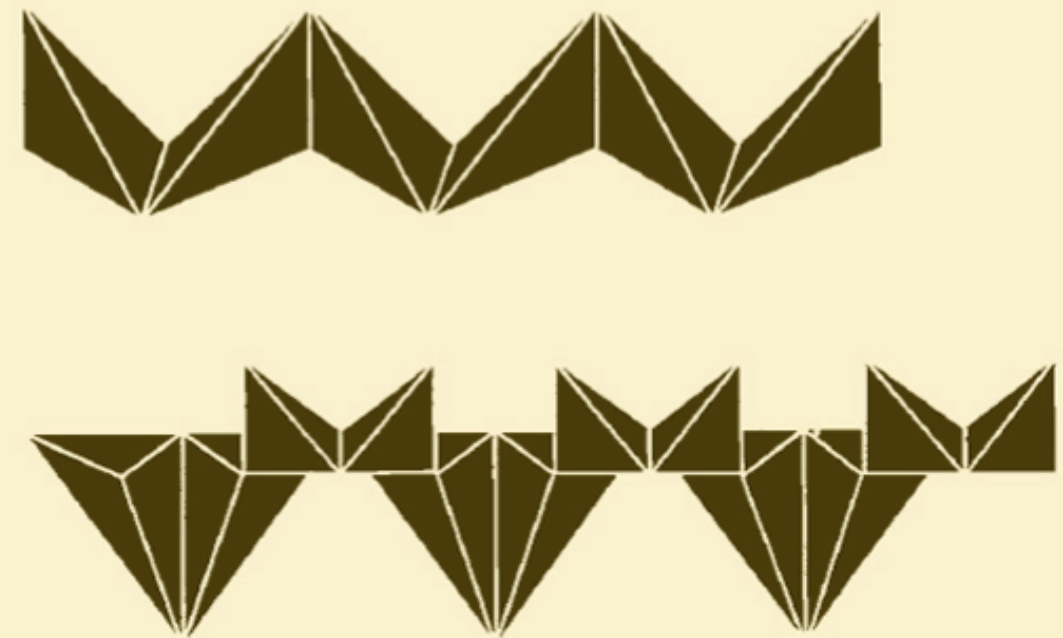
**Fig. 24**



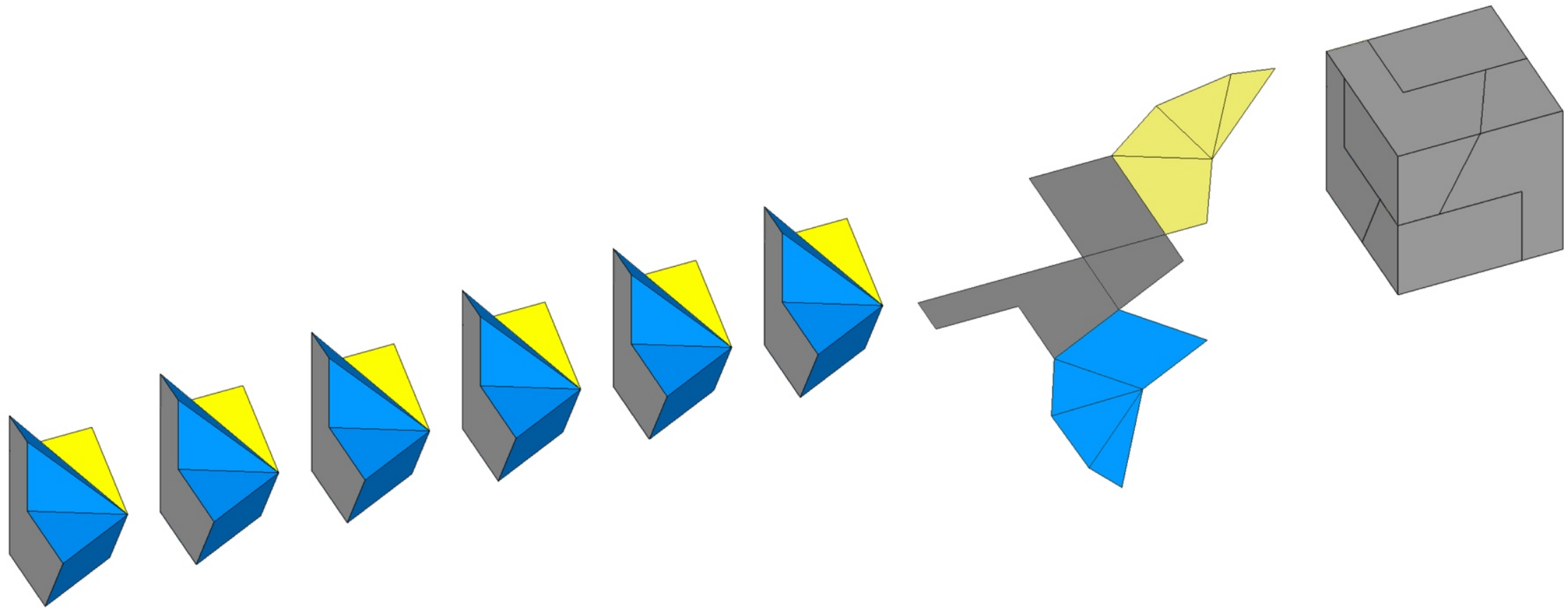
## THE CHAINS OF PAIRS OF SPECULAR MODULES

1. The tetrahedron, the cube..., all polyhedra, can be considered as one of the numerous three-dimensional configurations resulting from the folding of flexible chains of modules.

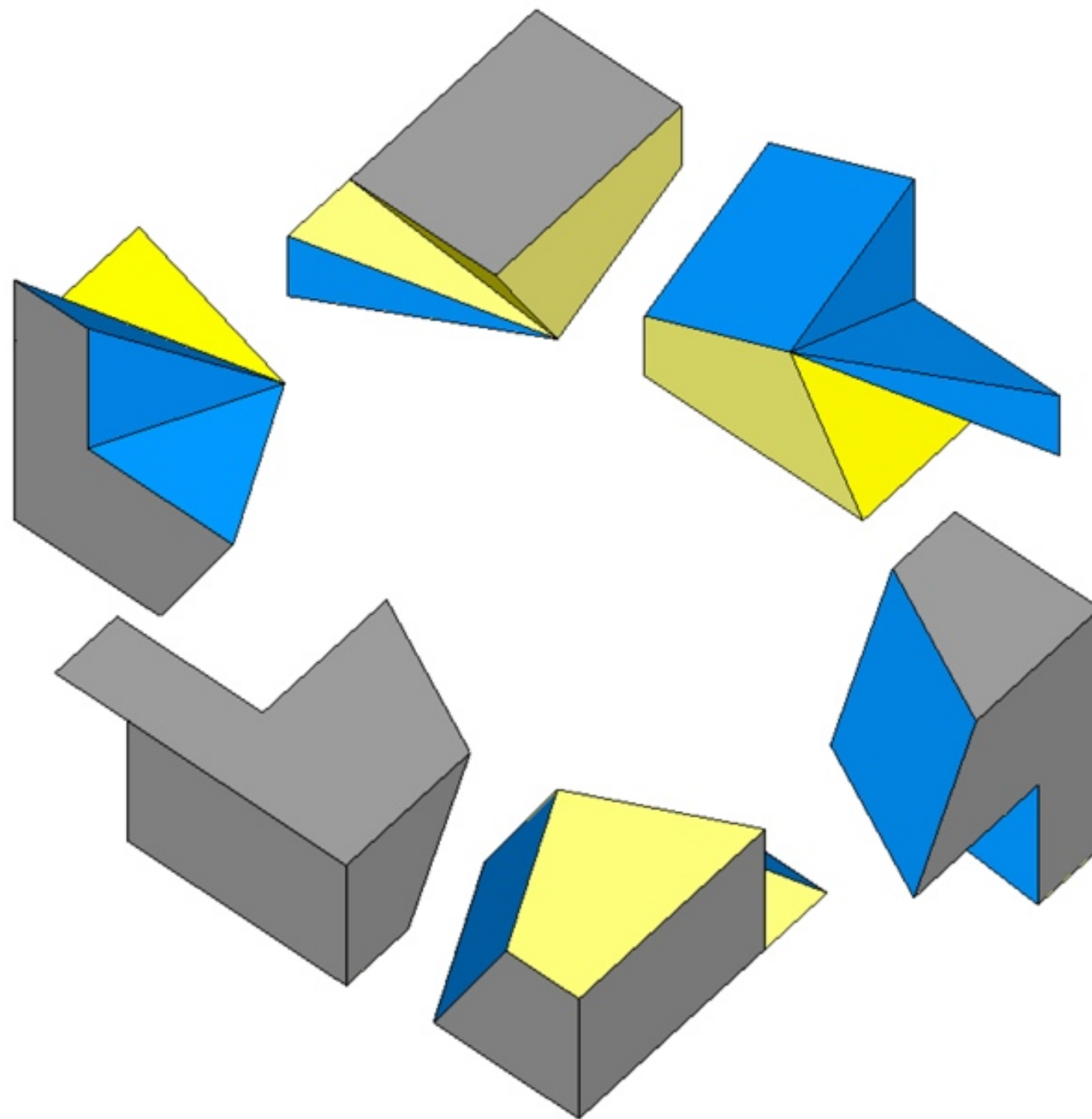
2. The chains are constituted by pairs of modules in which one component is the mirror image of the other.



**Fig. 25**

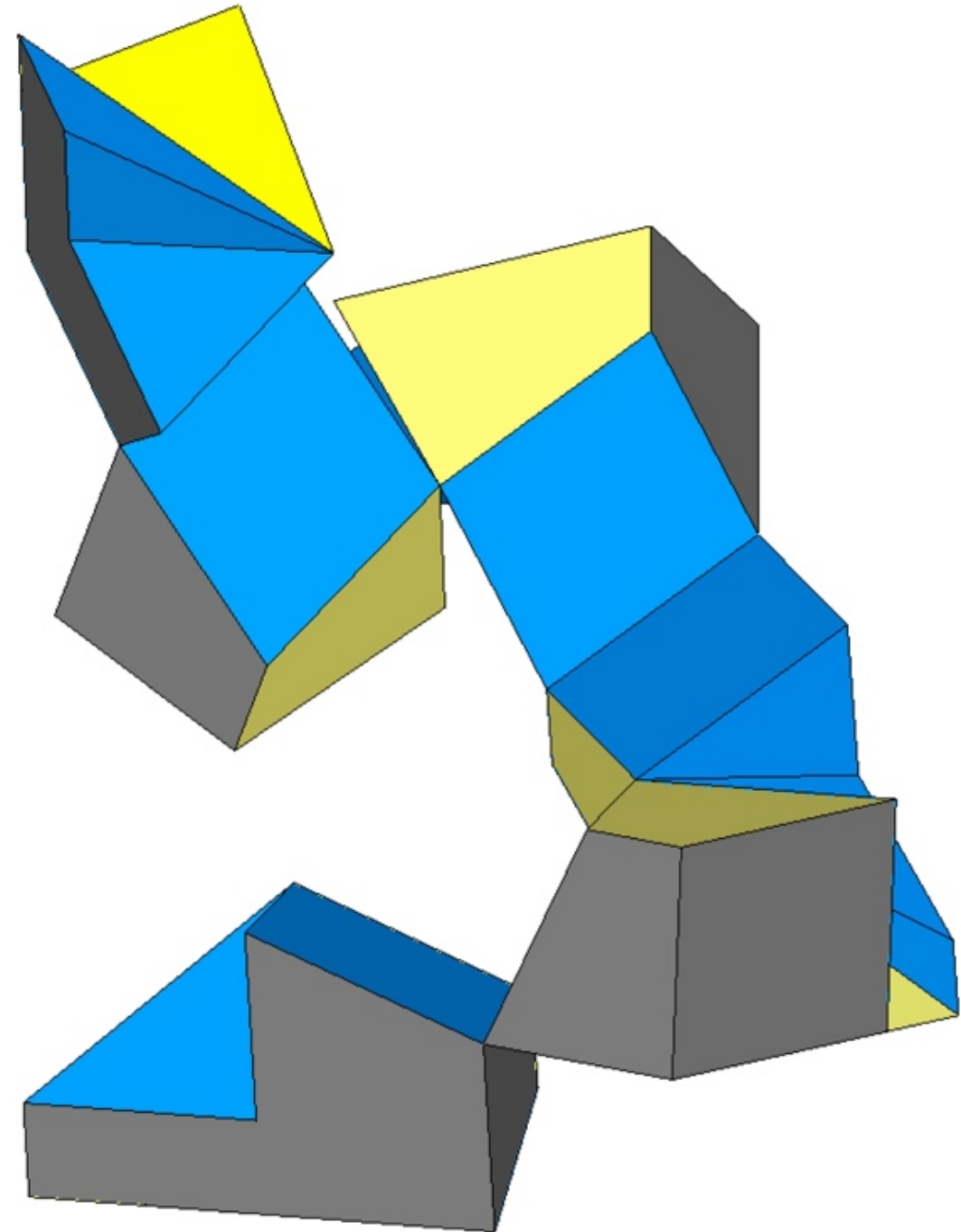
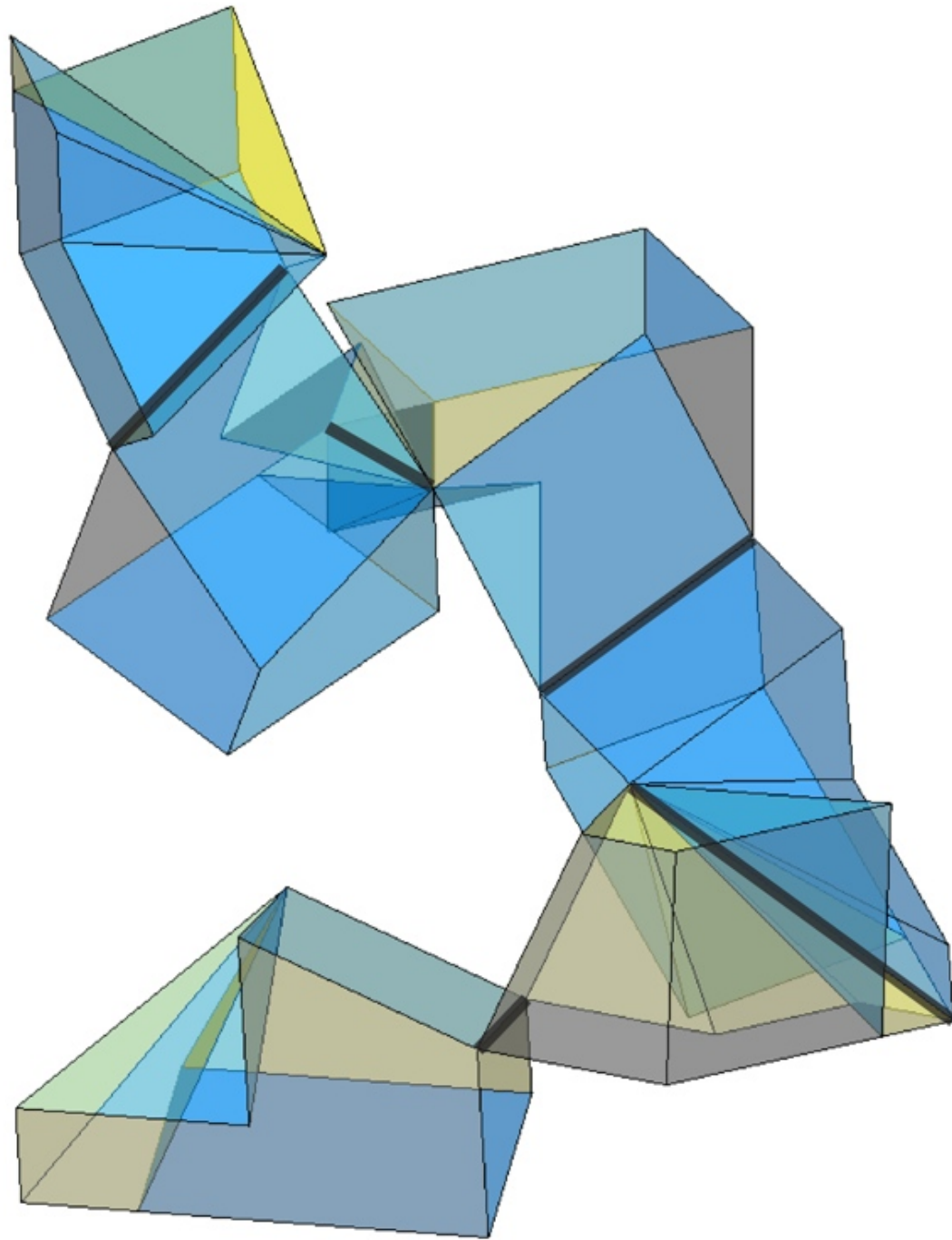


**Fig. 26**



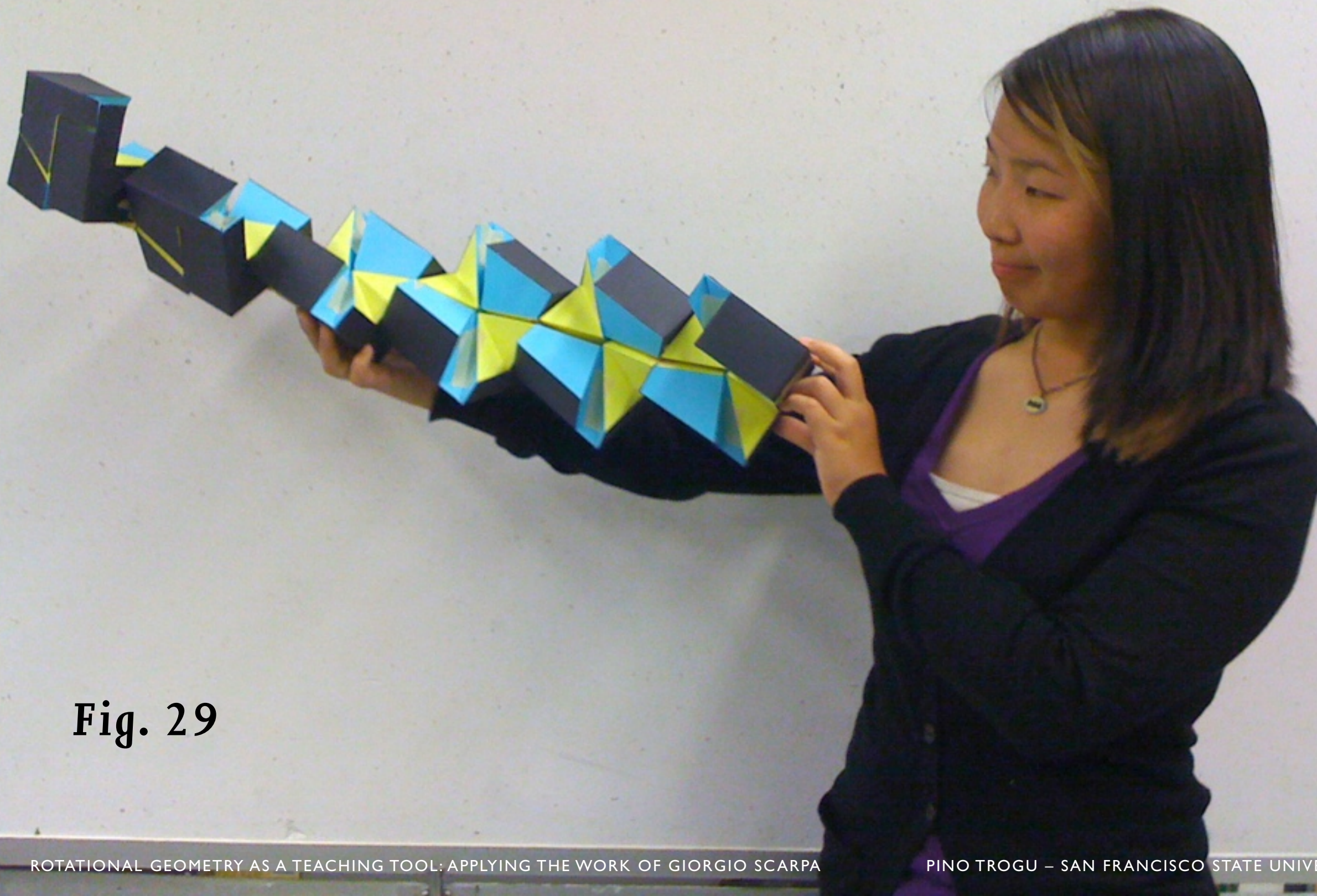
**Fig. 27**





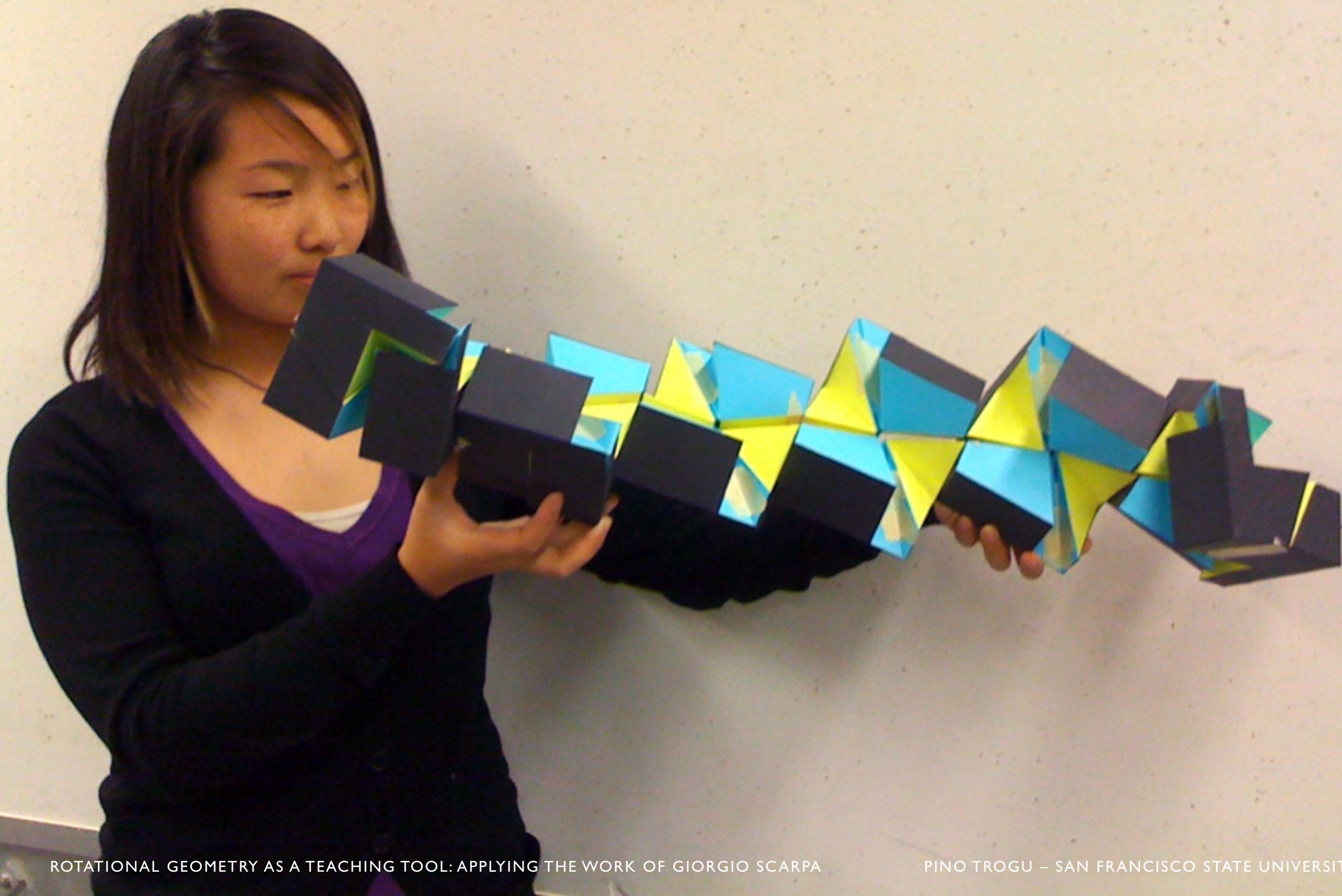
**Fig. 28**



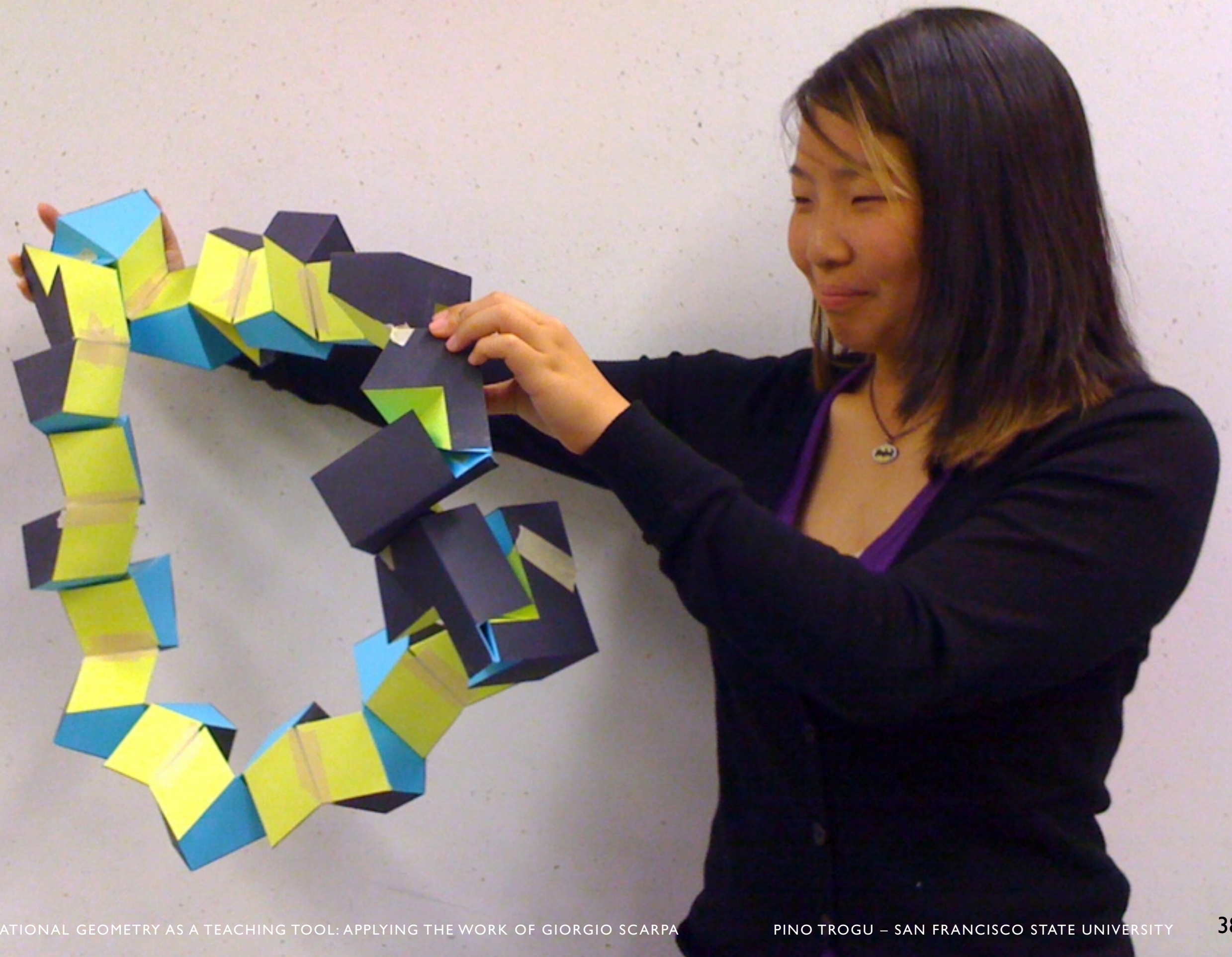


**Fig. 29**

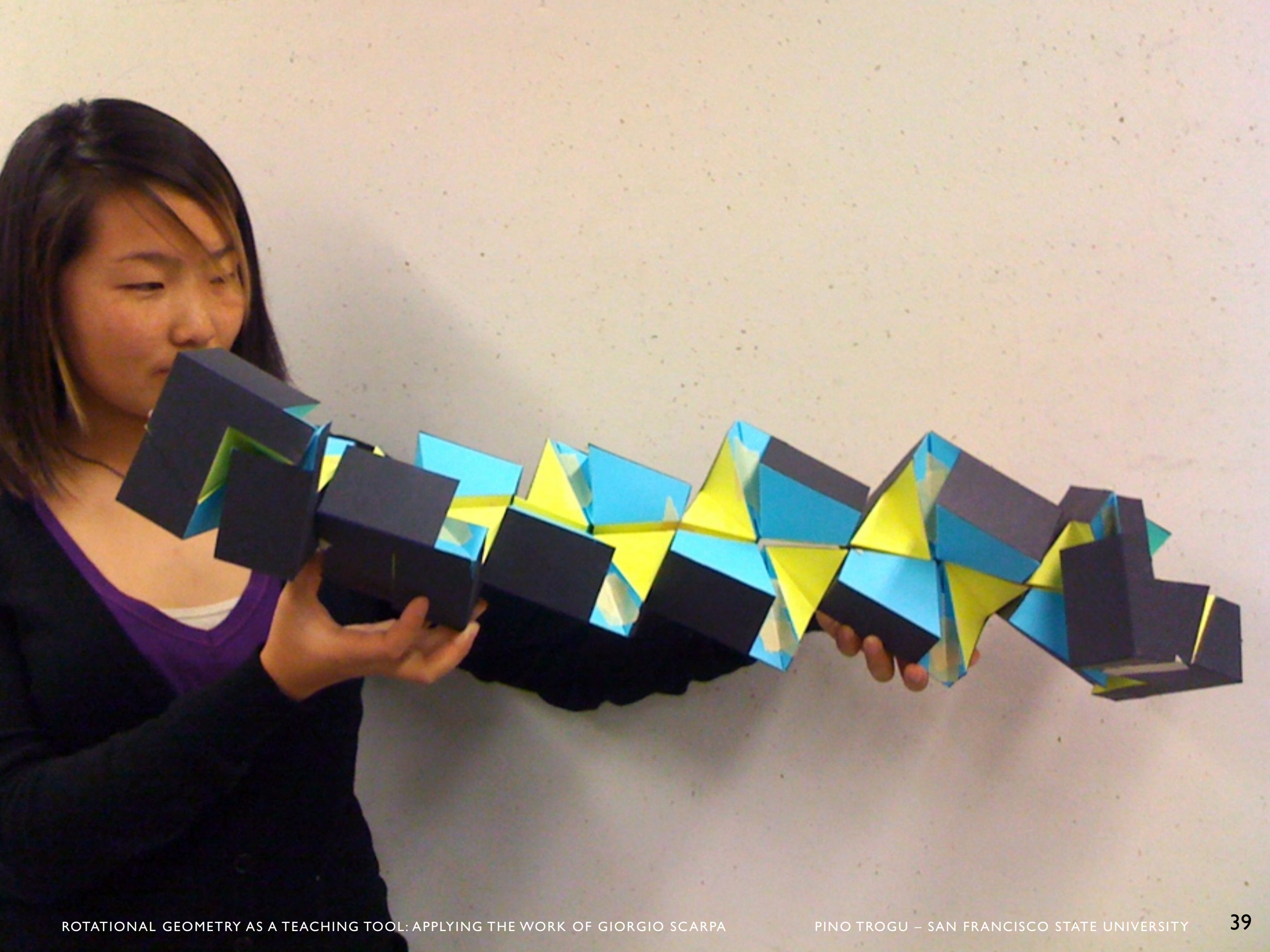




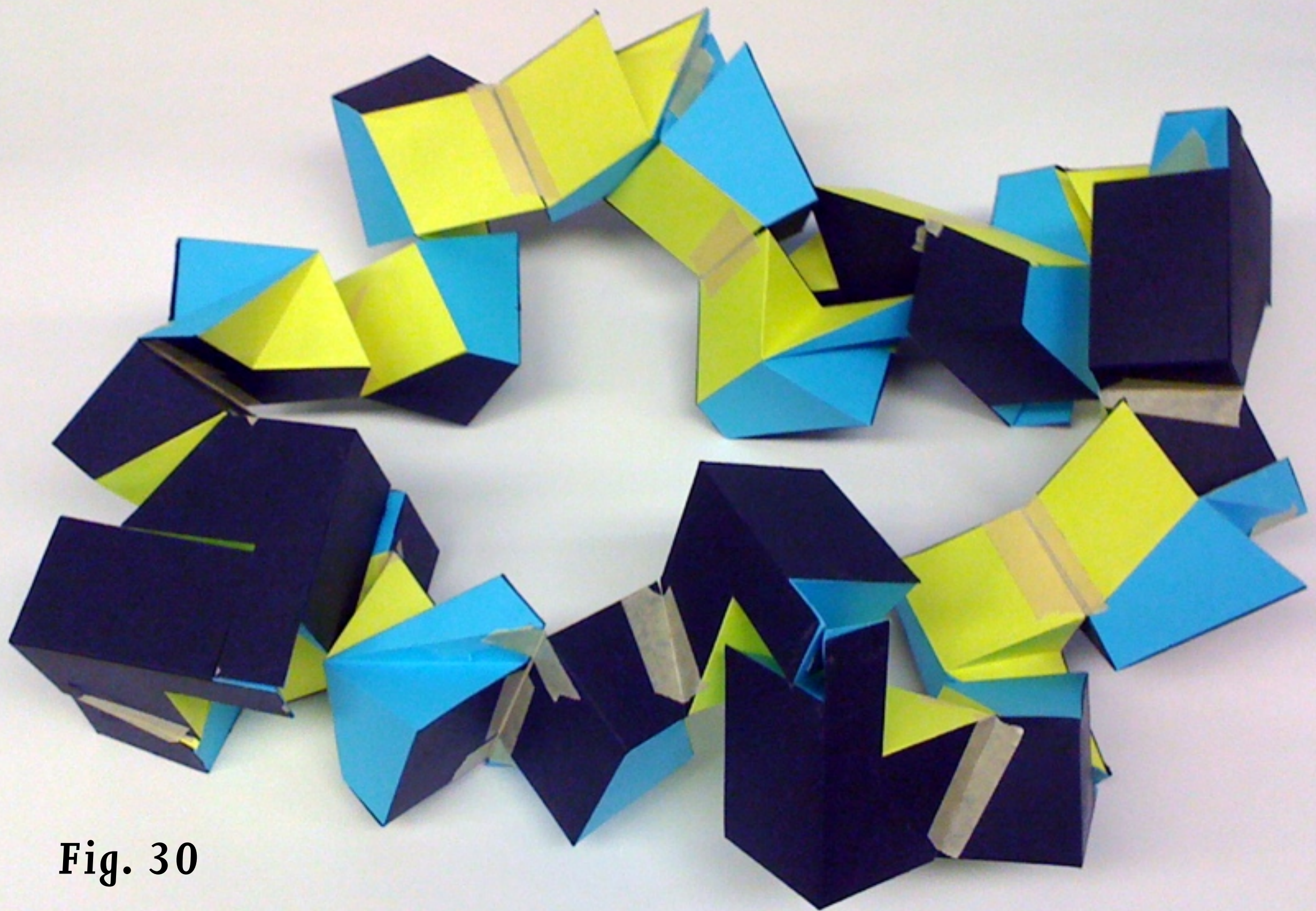






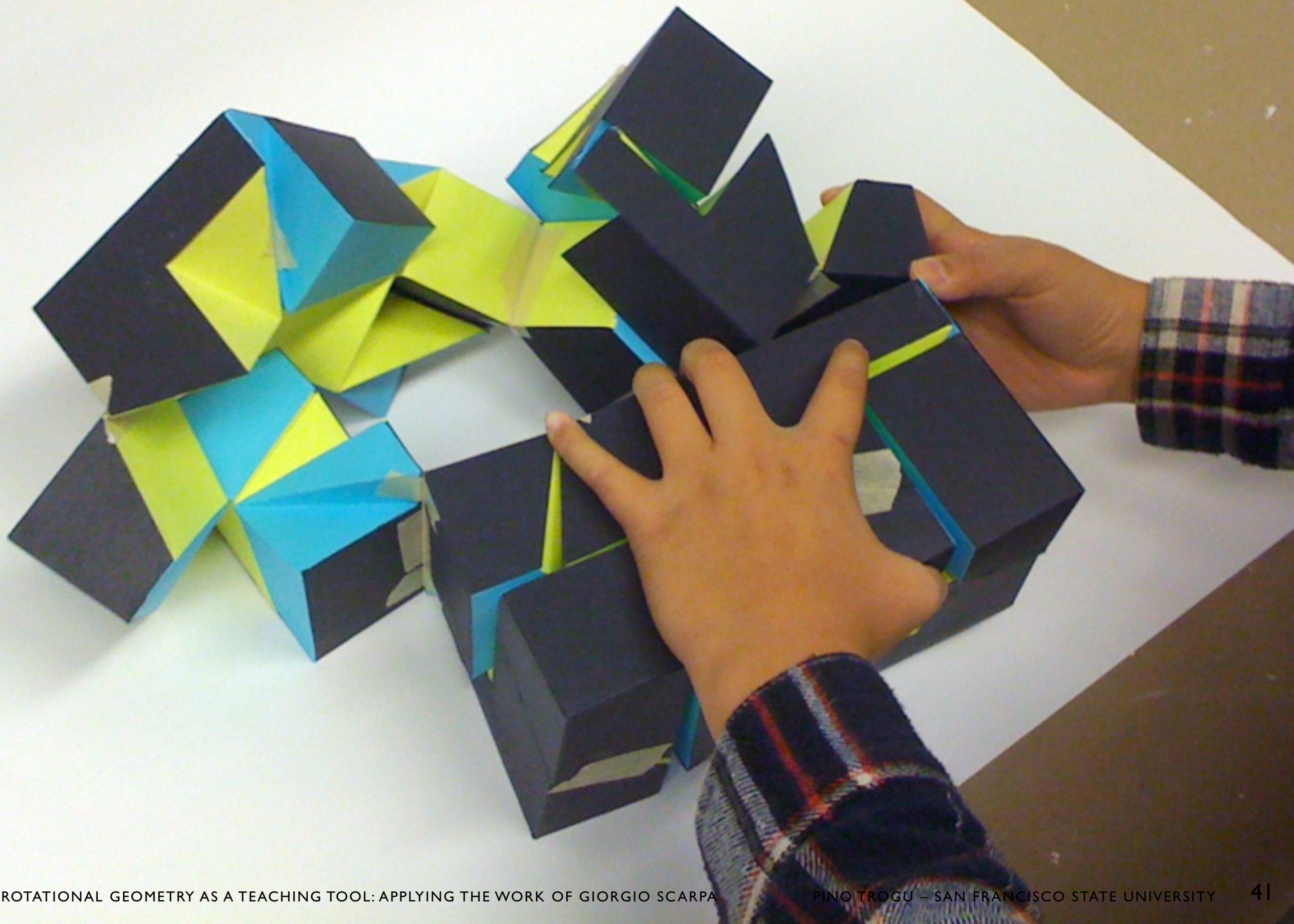




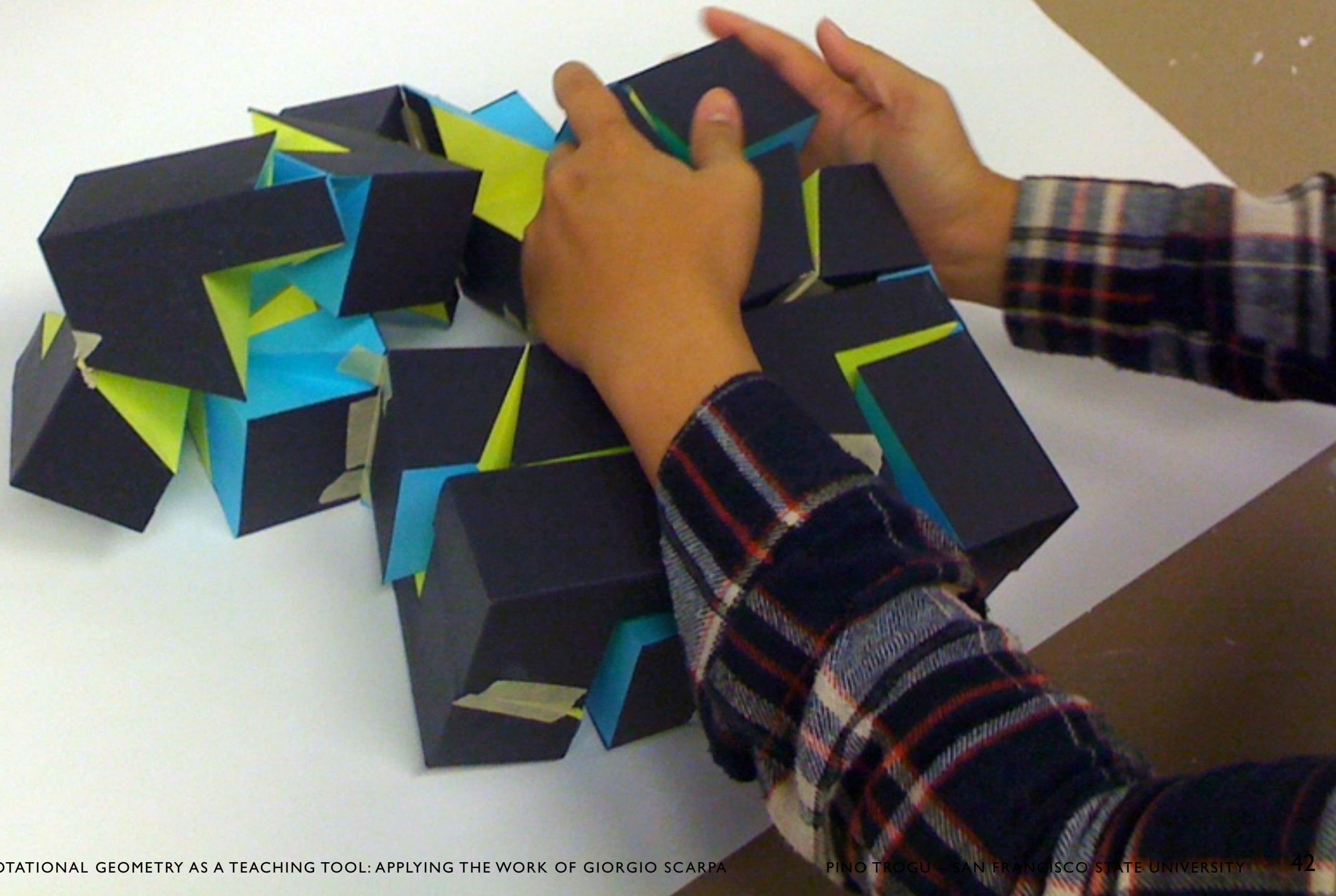


**Fig. 30**

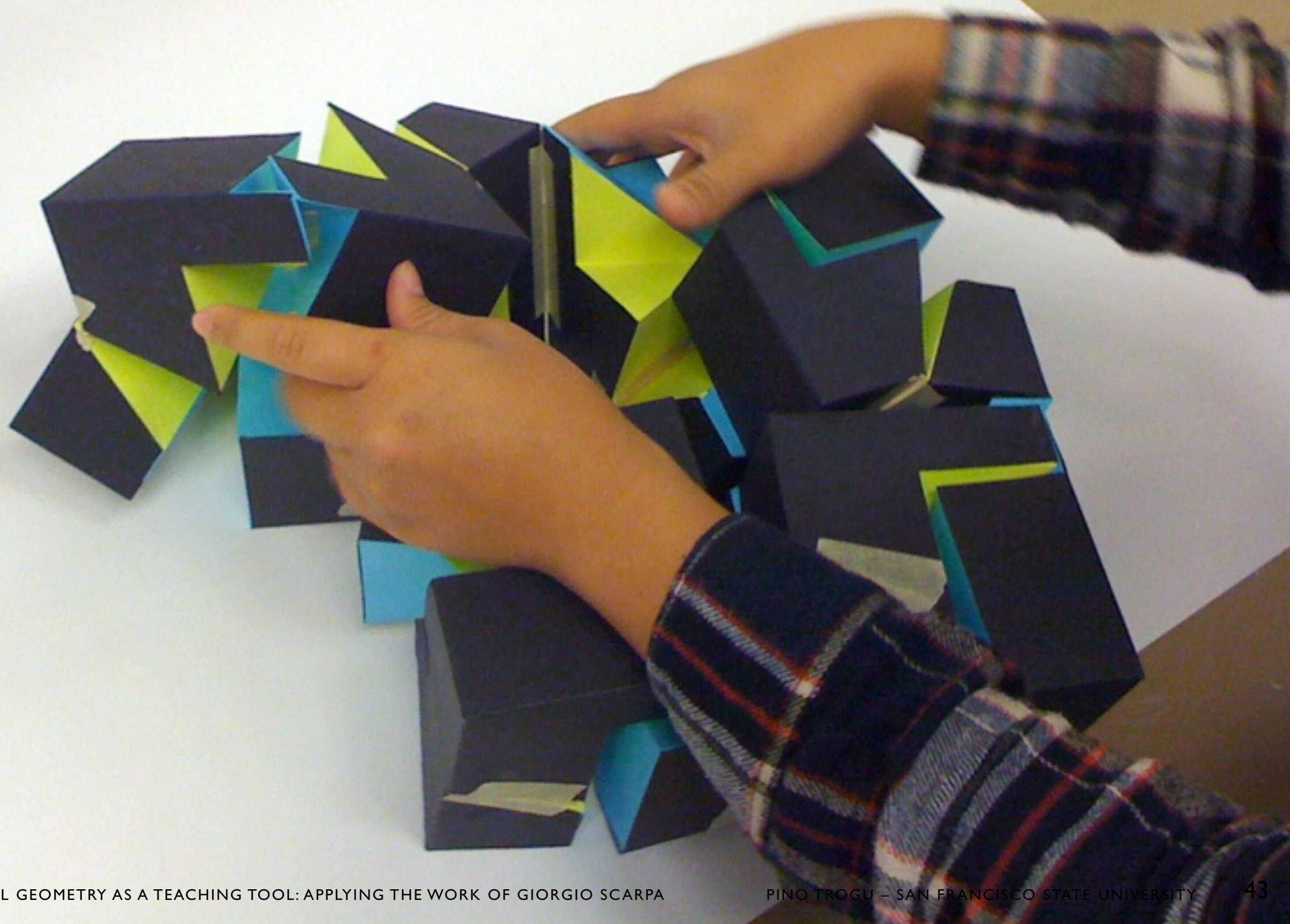




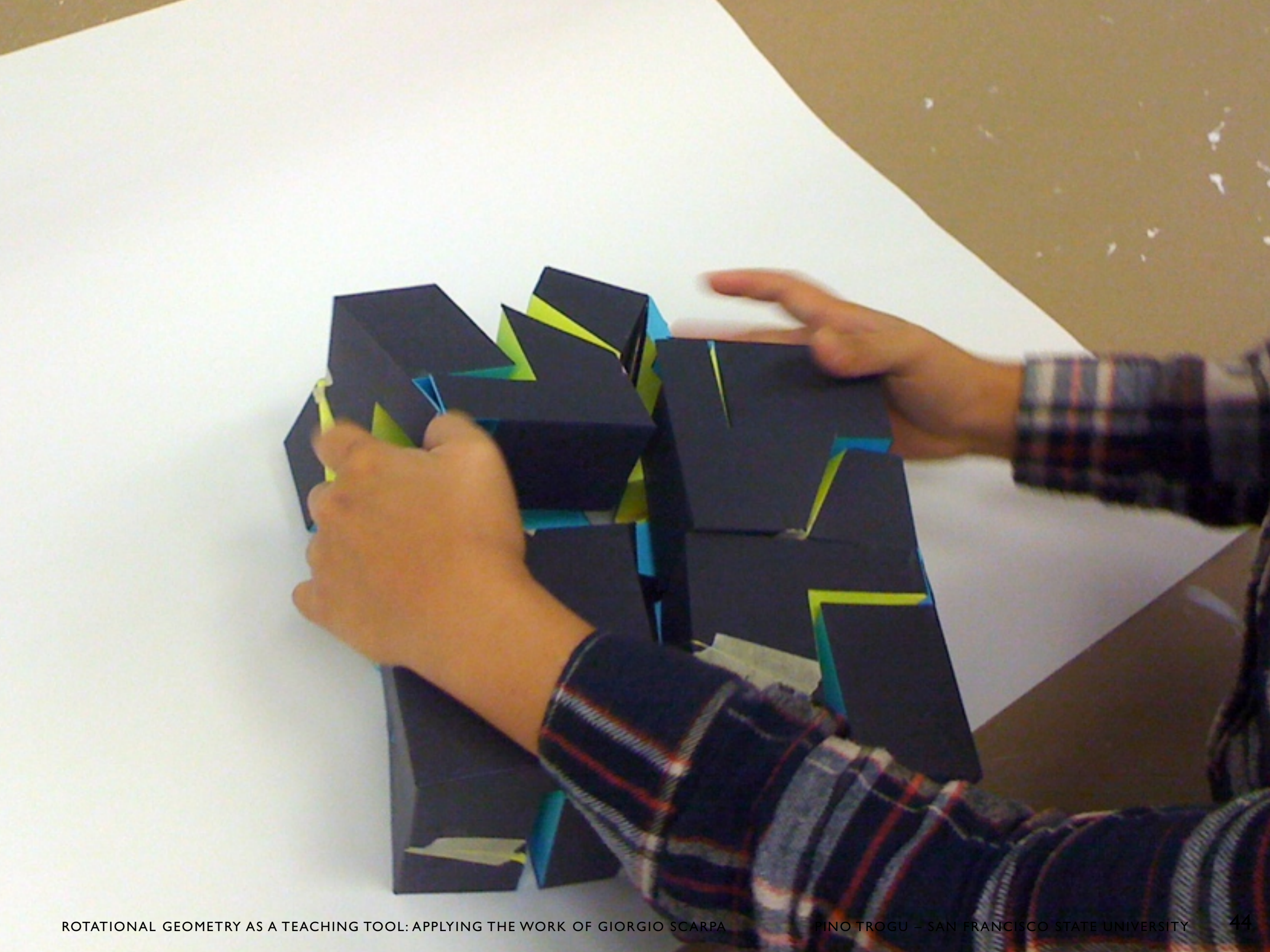








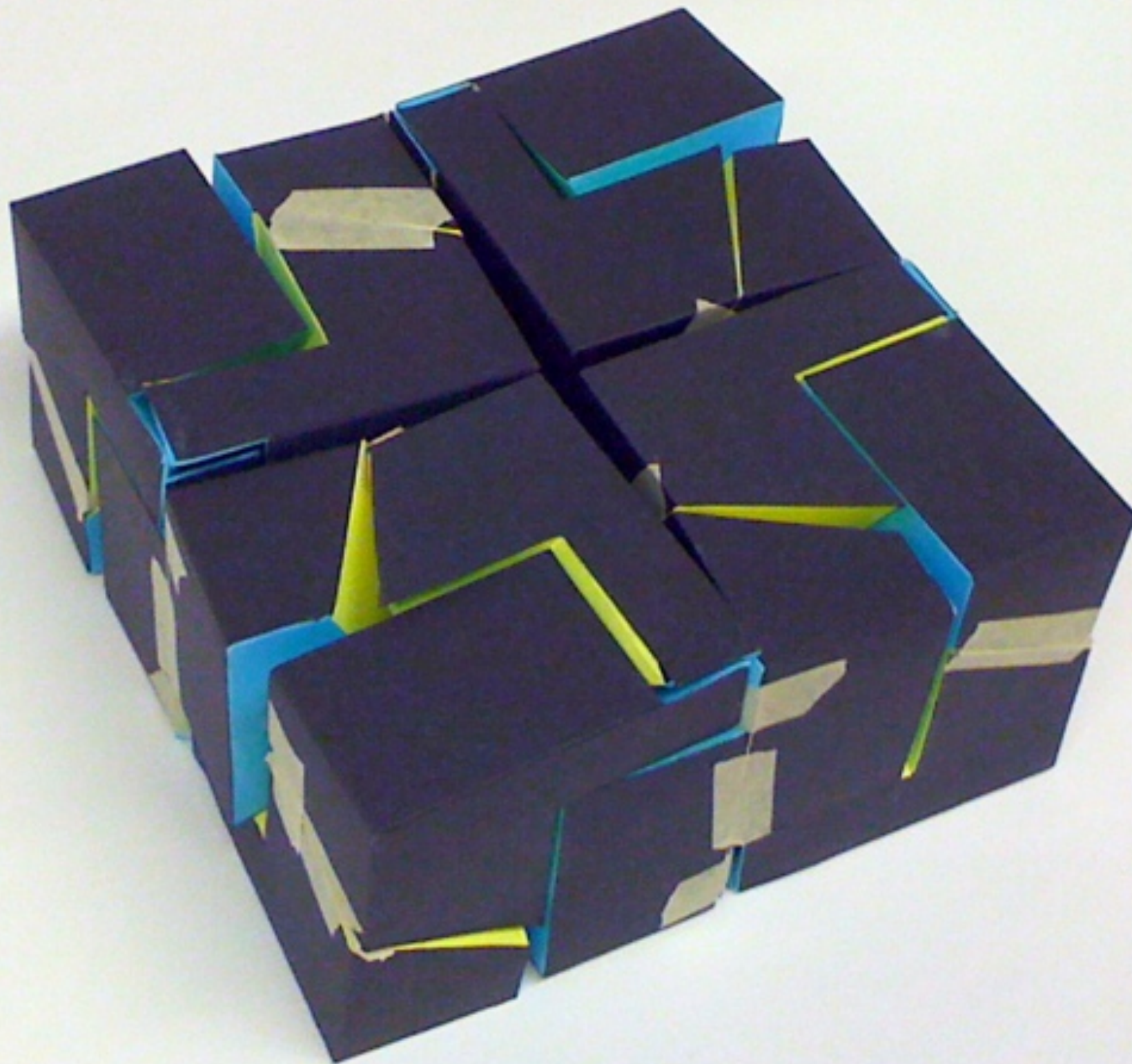










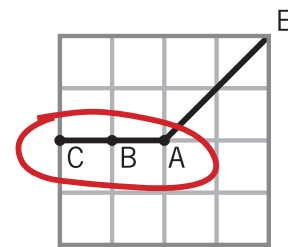




# CUBE SECTION – INTERNAL SURFACE

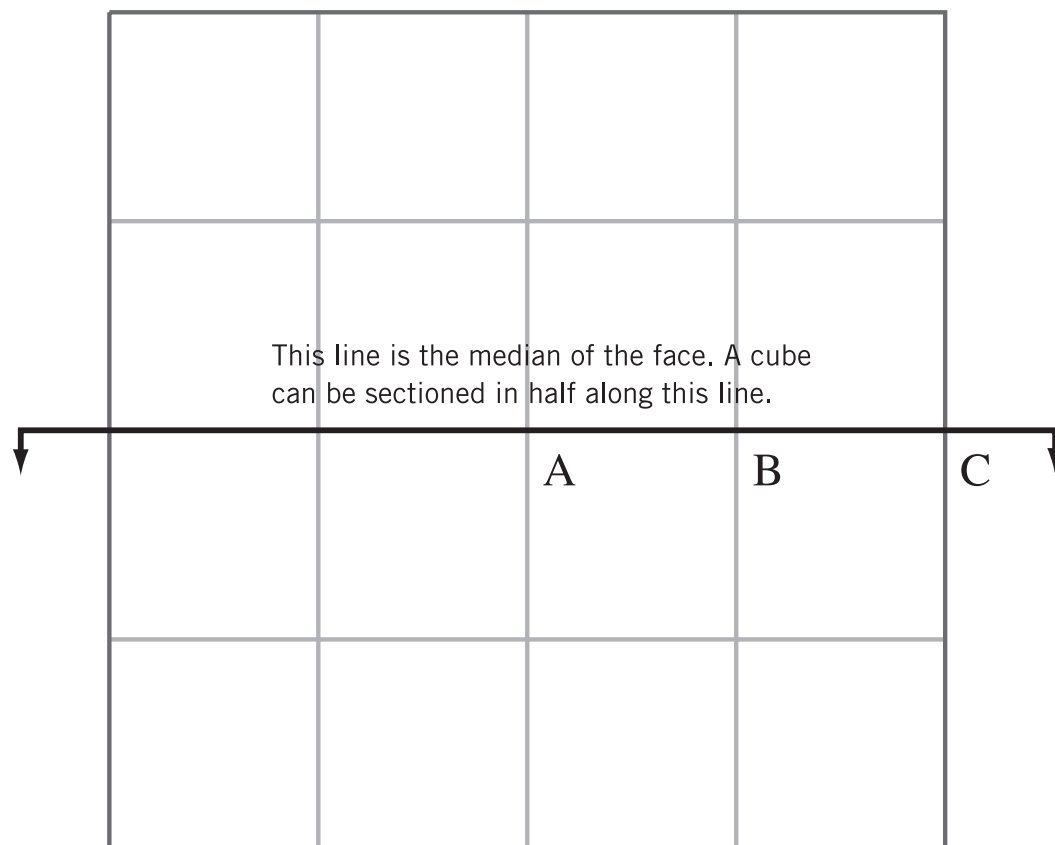
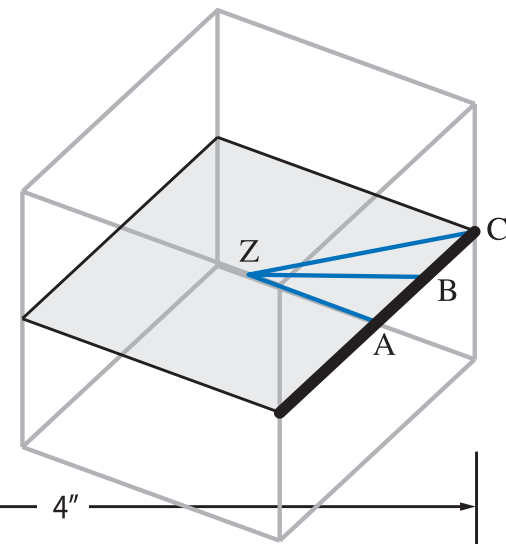
**Step 4** Use the given letters to mark any external points of the section that are either on the median or...

**NOTE:** when printing, select Page Scaling: NONE. Check your drawing after printing to verify dimensions. Check both axes: vertical and horizontal.



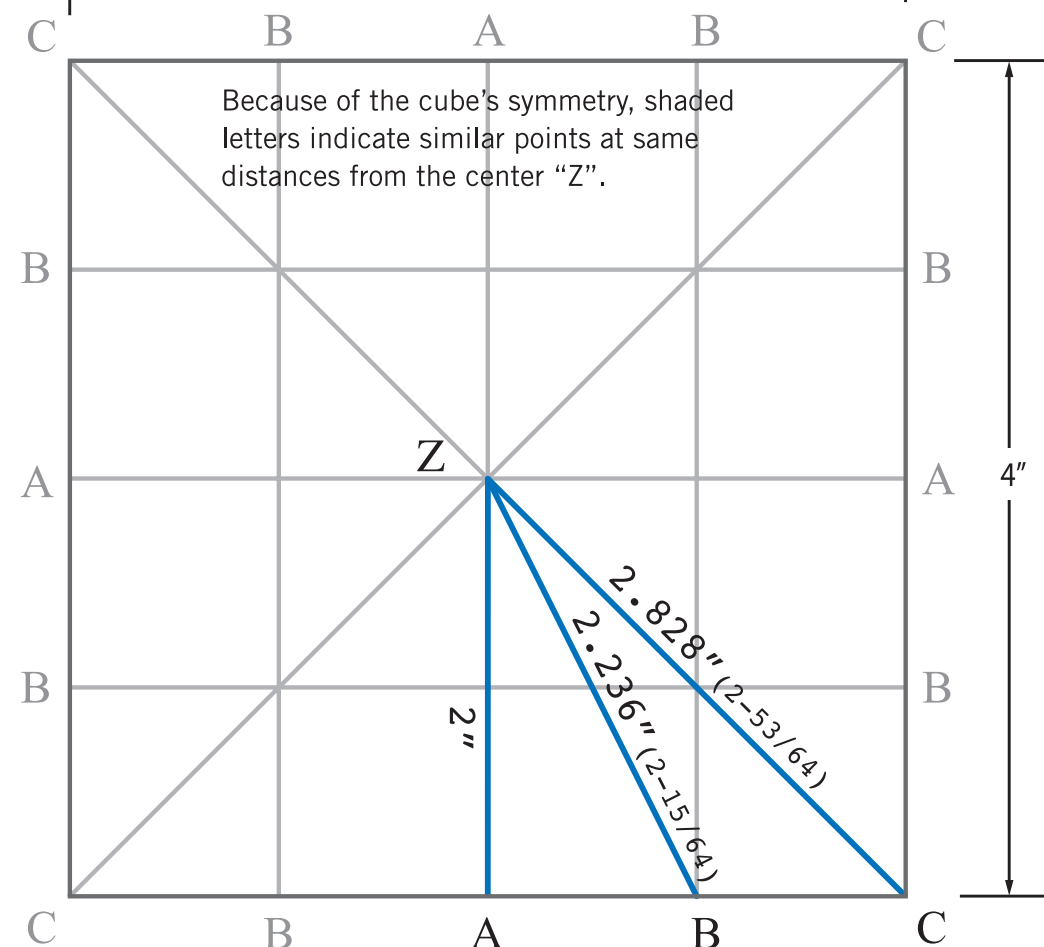
Use this page to find distances for points "A", "B", and "C".

Distances from points on the median to the center of the cube "Z".



Face of the cube sectioned along the median.

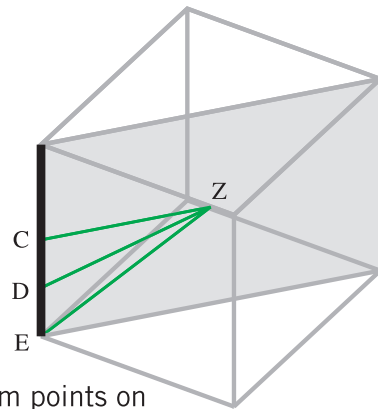
**NOTE:** You can use this grid to draw your section at full scale.



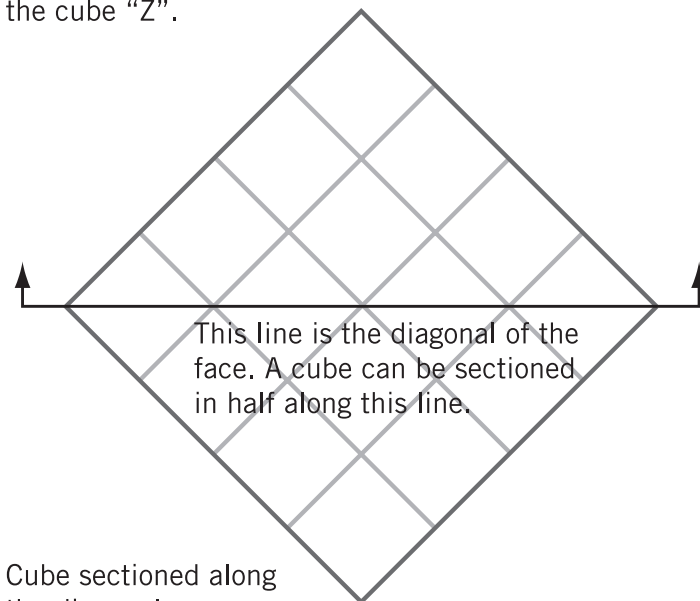
# CUBE SECTION – INTERNAL SURFACE

## Step 4 ...the edge of the face/cube.

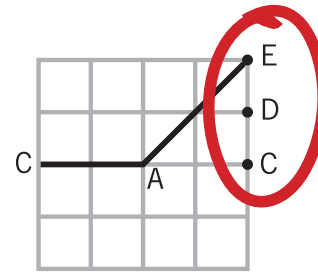
**NOTE:** when printing, select Page Scaling: NONE.  
Check your drawing after printing to verify dimensions.  
Check both axes: vertical and horizontal.



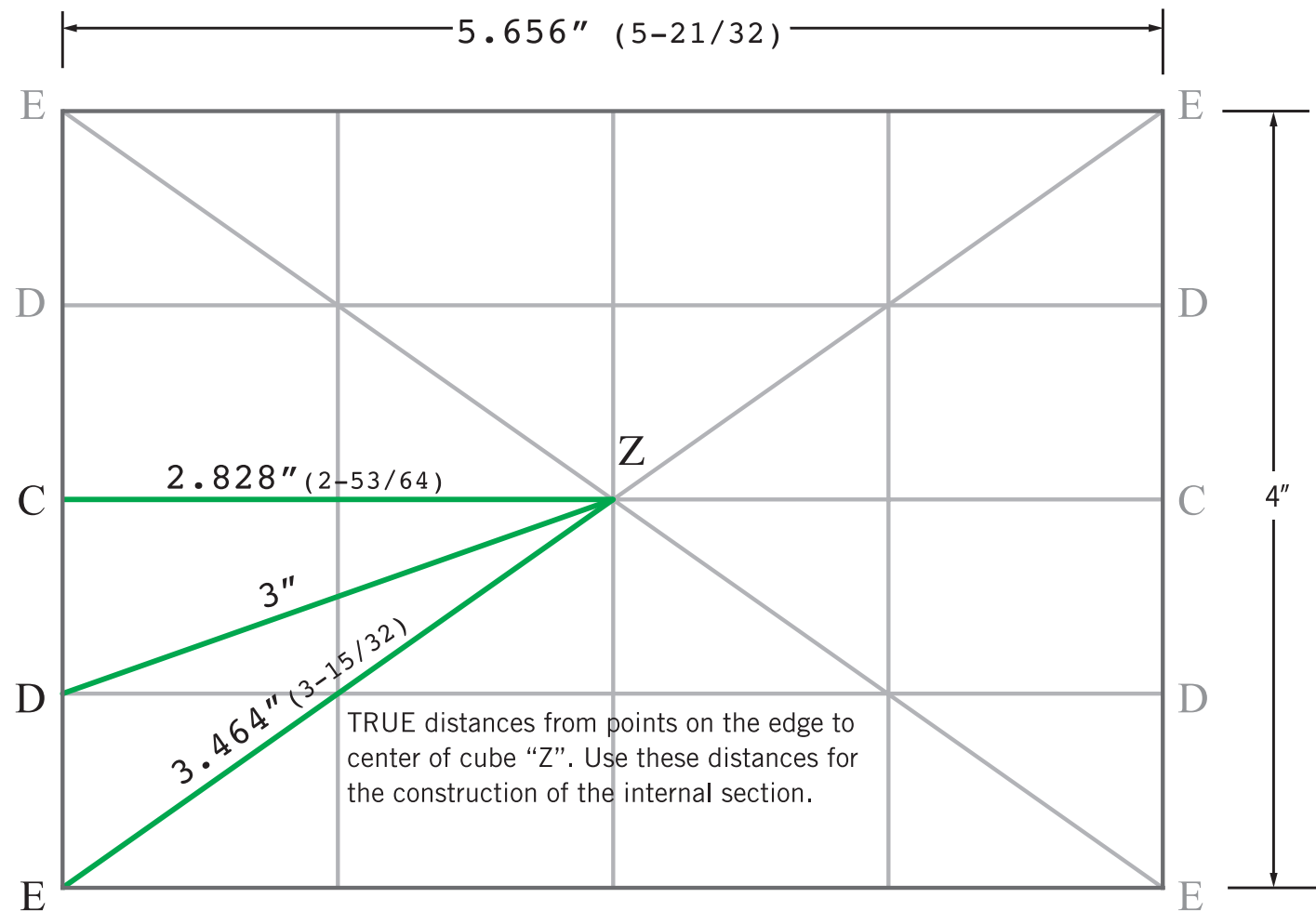
Distances from points on the edge to the center of the cube "Z".



Cube sectioned along the diagonal.



Use this page to find distances for points "C", "D", and "E"



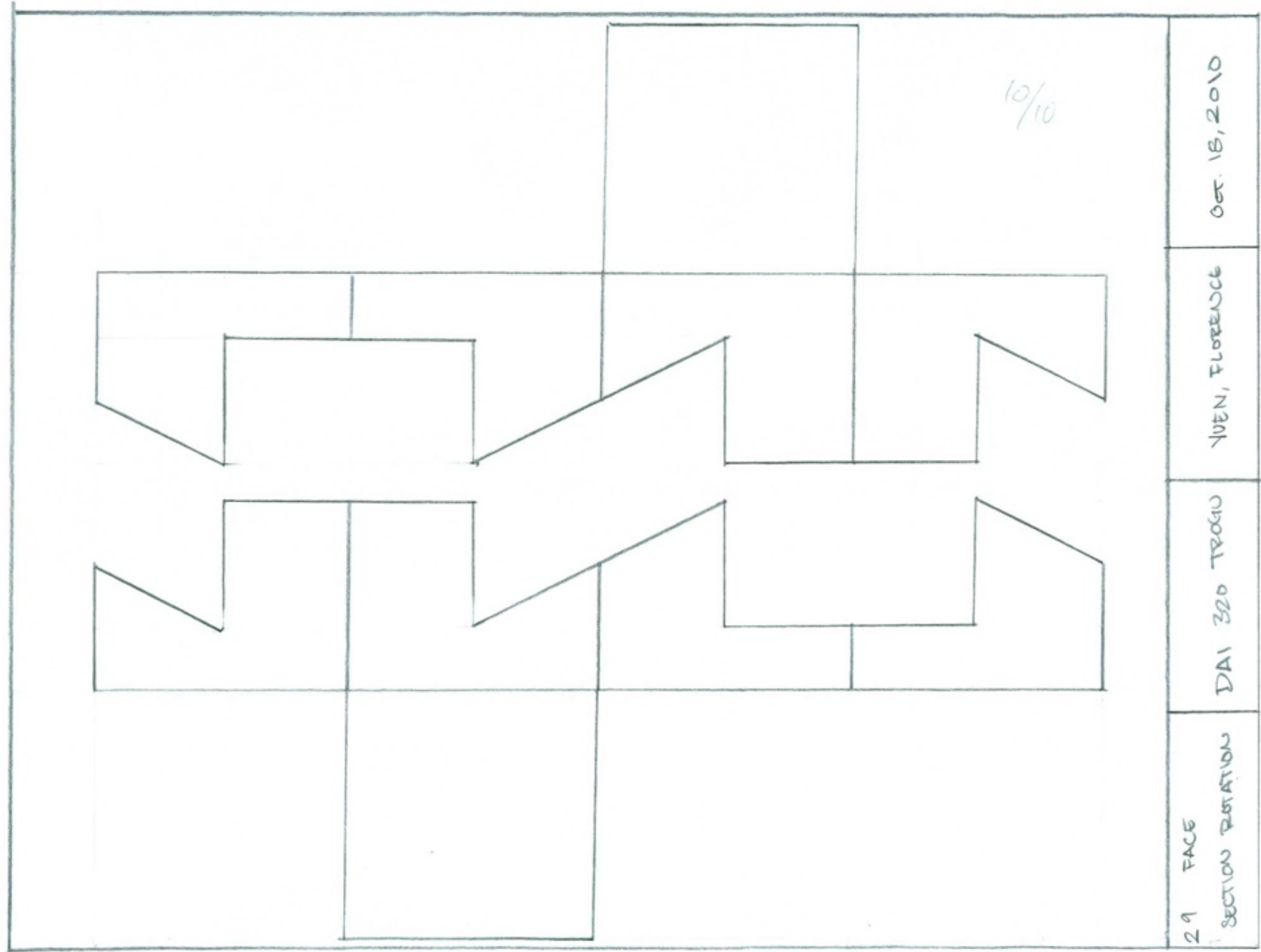


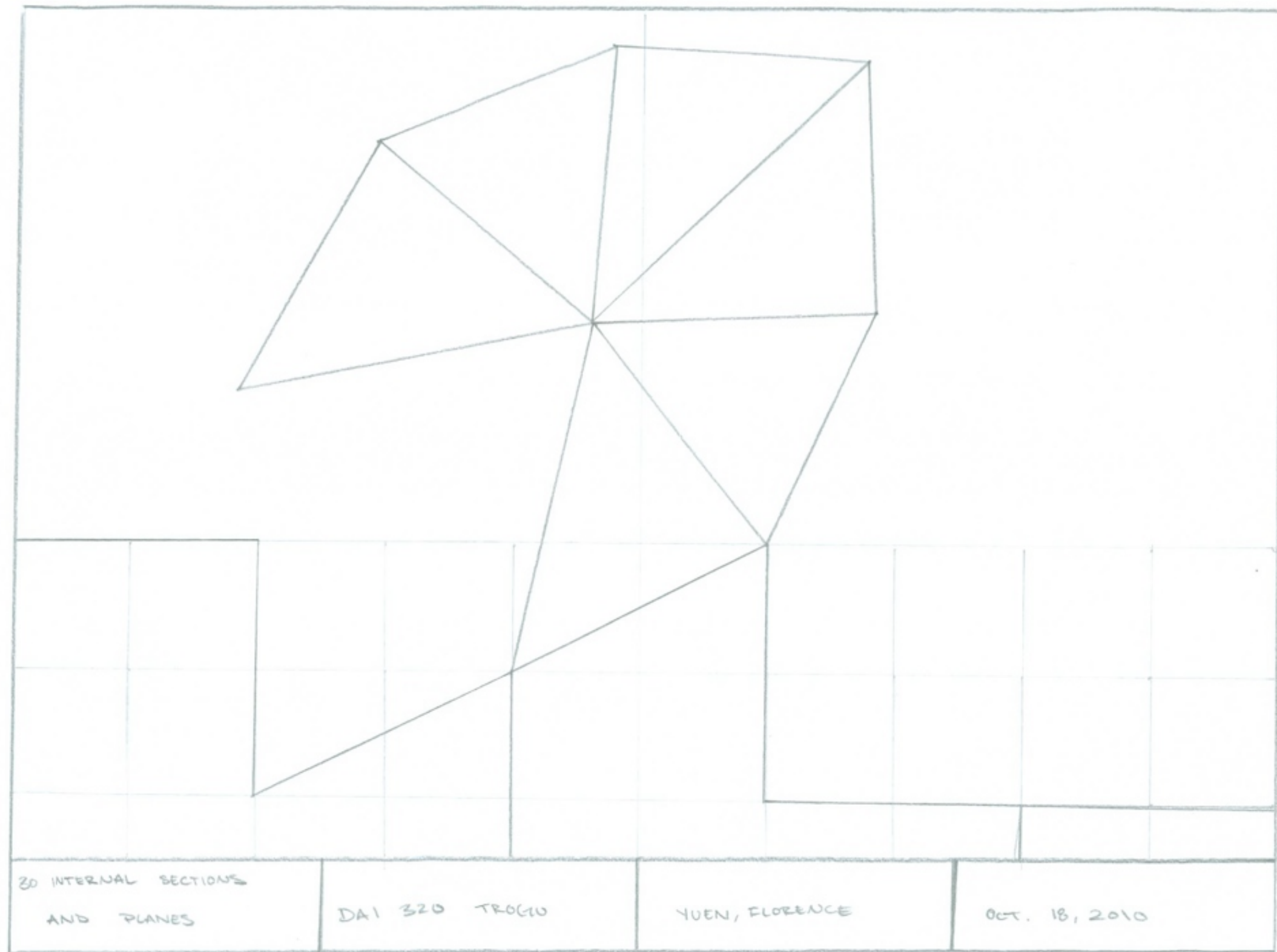




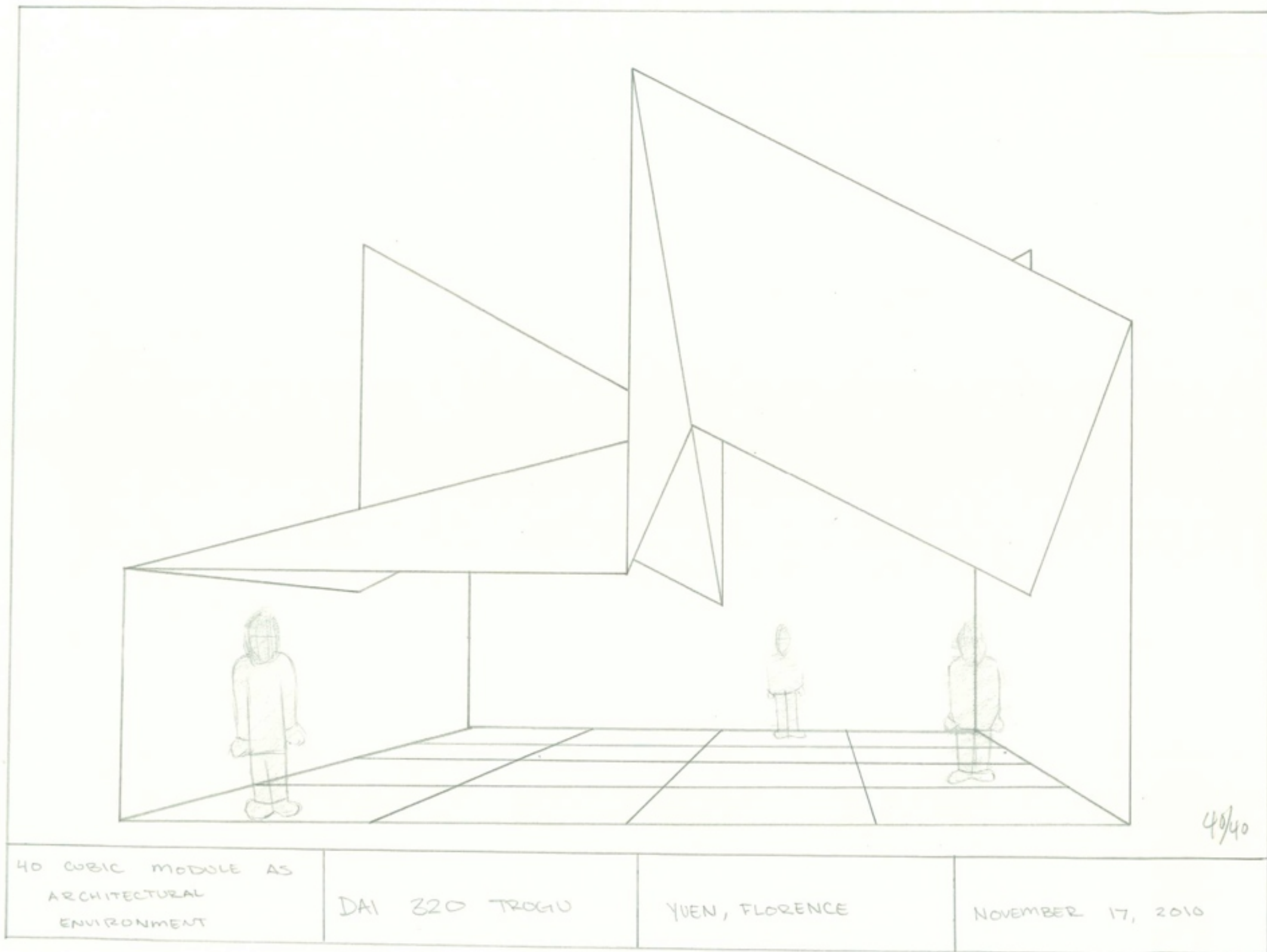


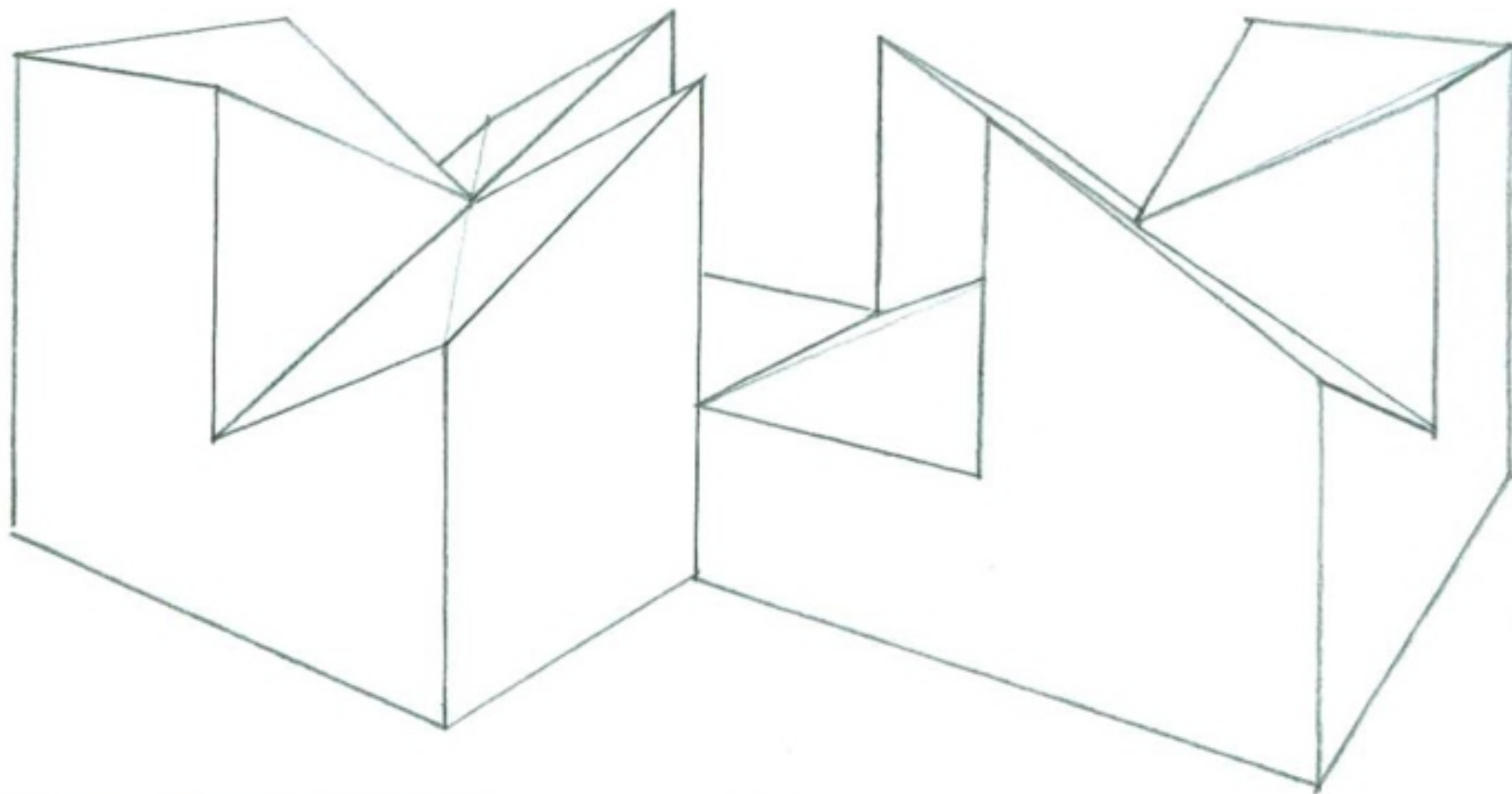












40  
/ 40

43 TWO CUBIC  
MODULES

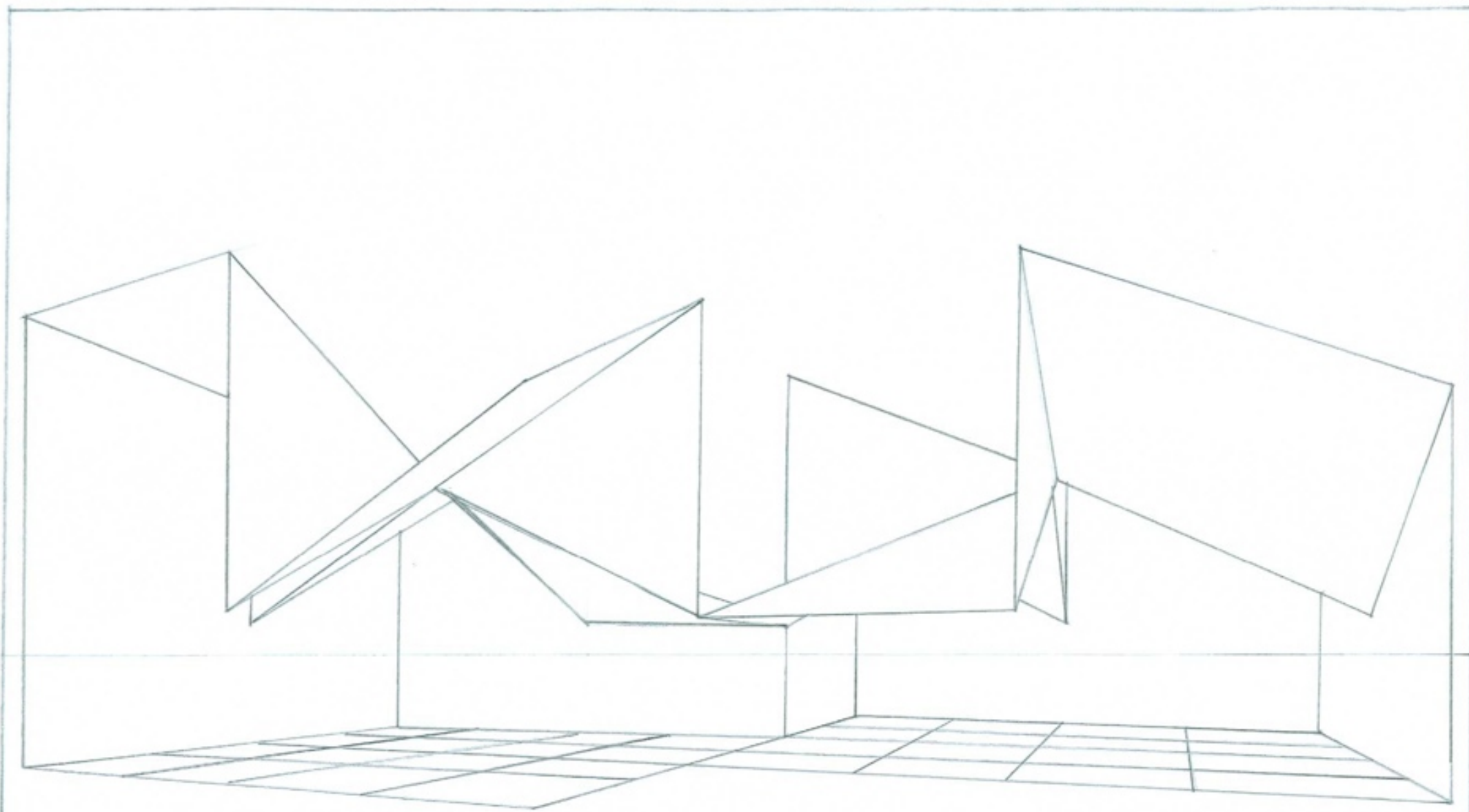
DAI 320 TROGU

YUEN, FLORENCE

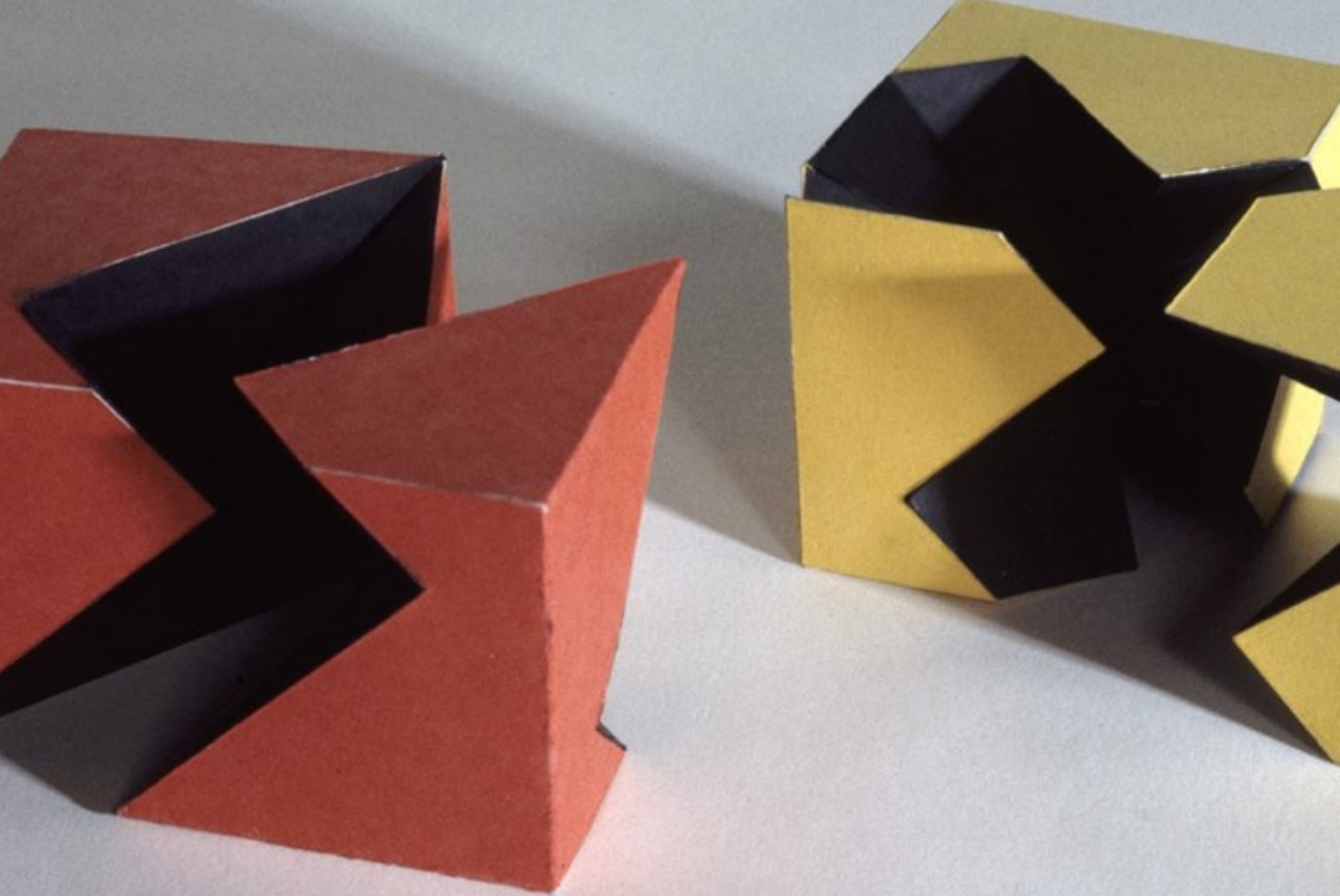
DEC. 13, 2010



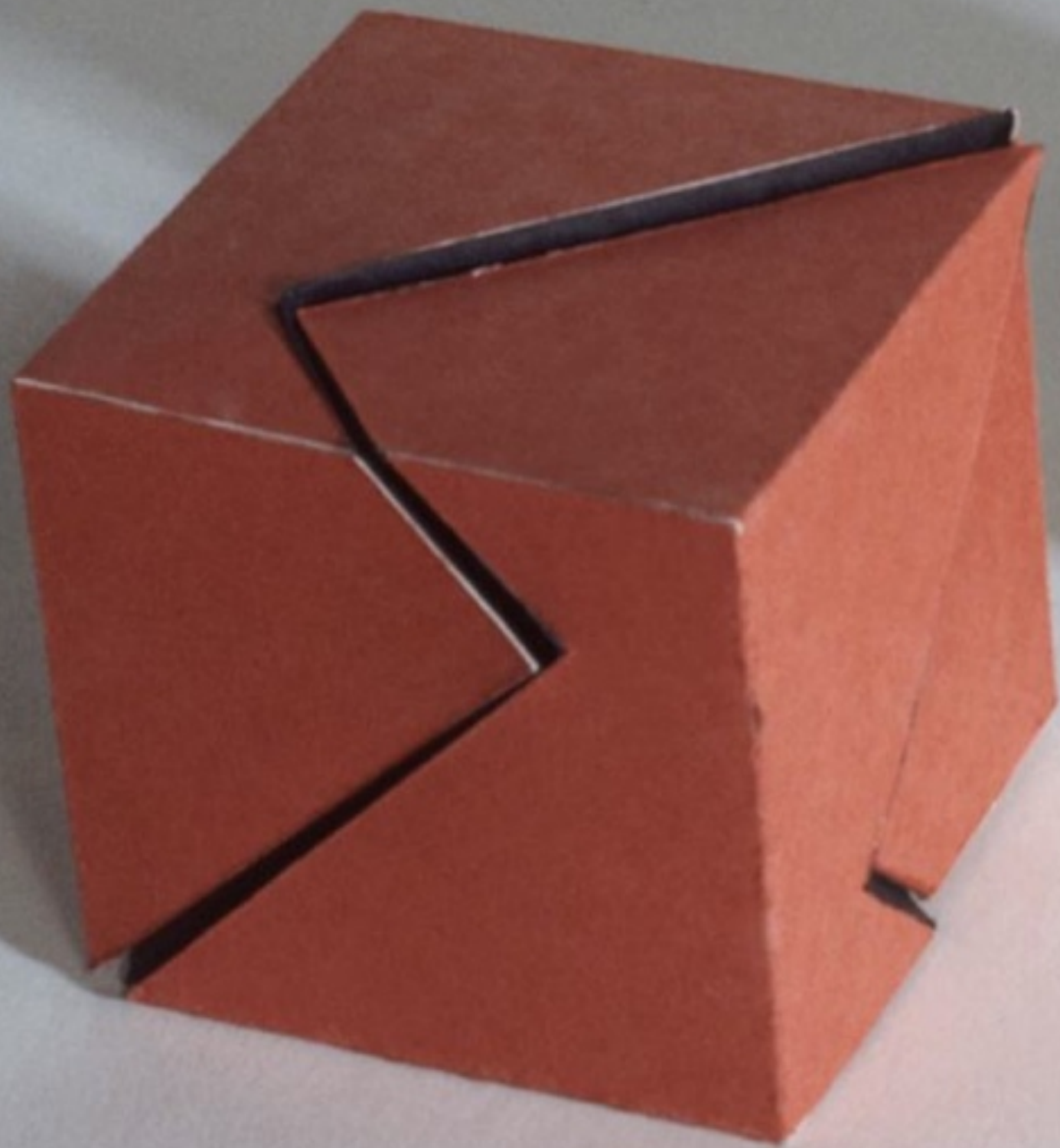
50/50



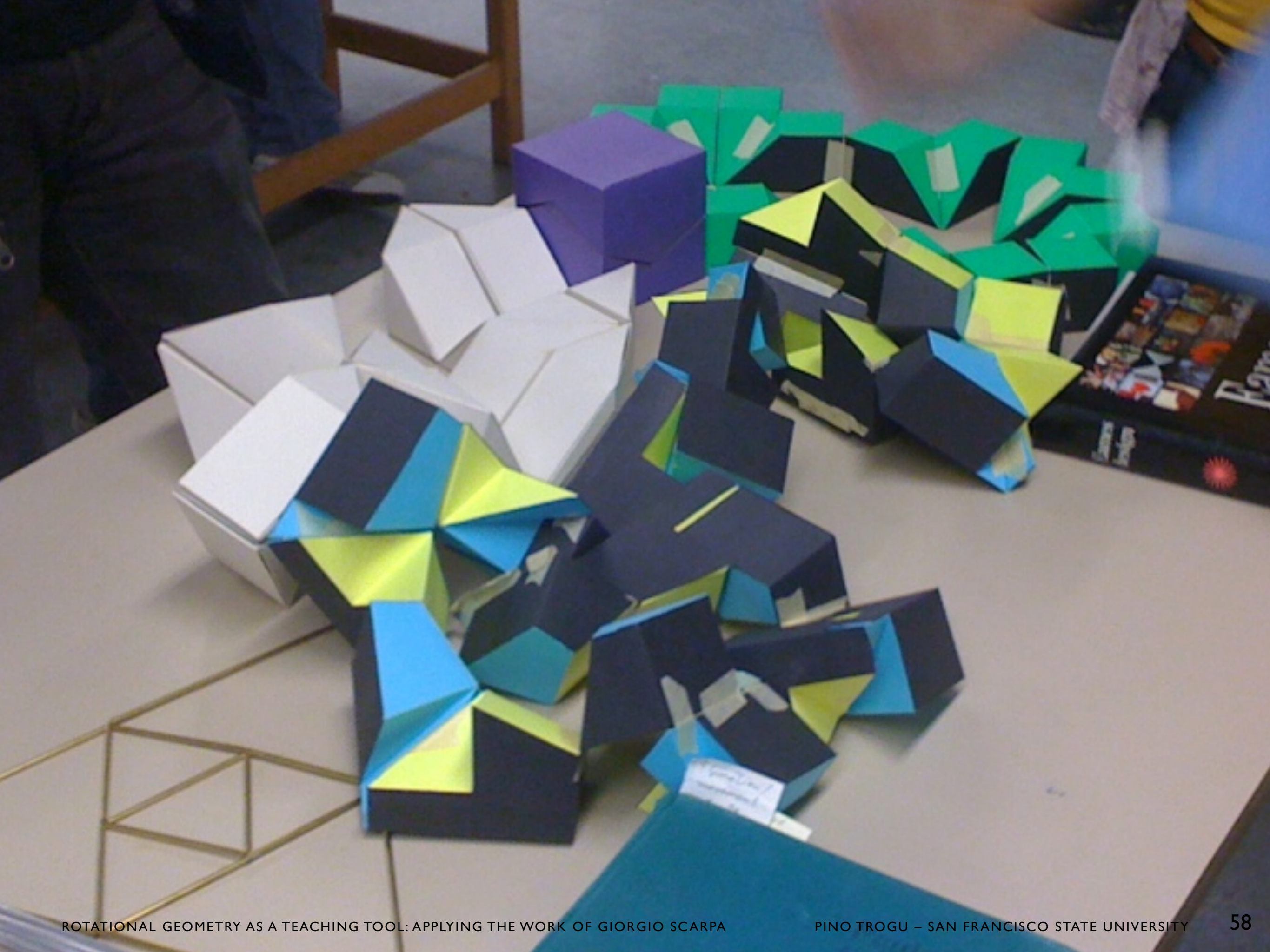
44 TWO CUBIC MODULES (LOWER H.L.)	DAI 320 TROGU	YUEN, FLORENCE	DEC 14, 2010
--------------------------------------	---------------	----------------	--------------



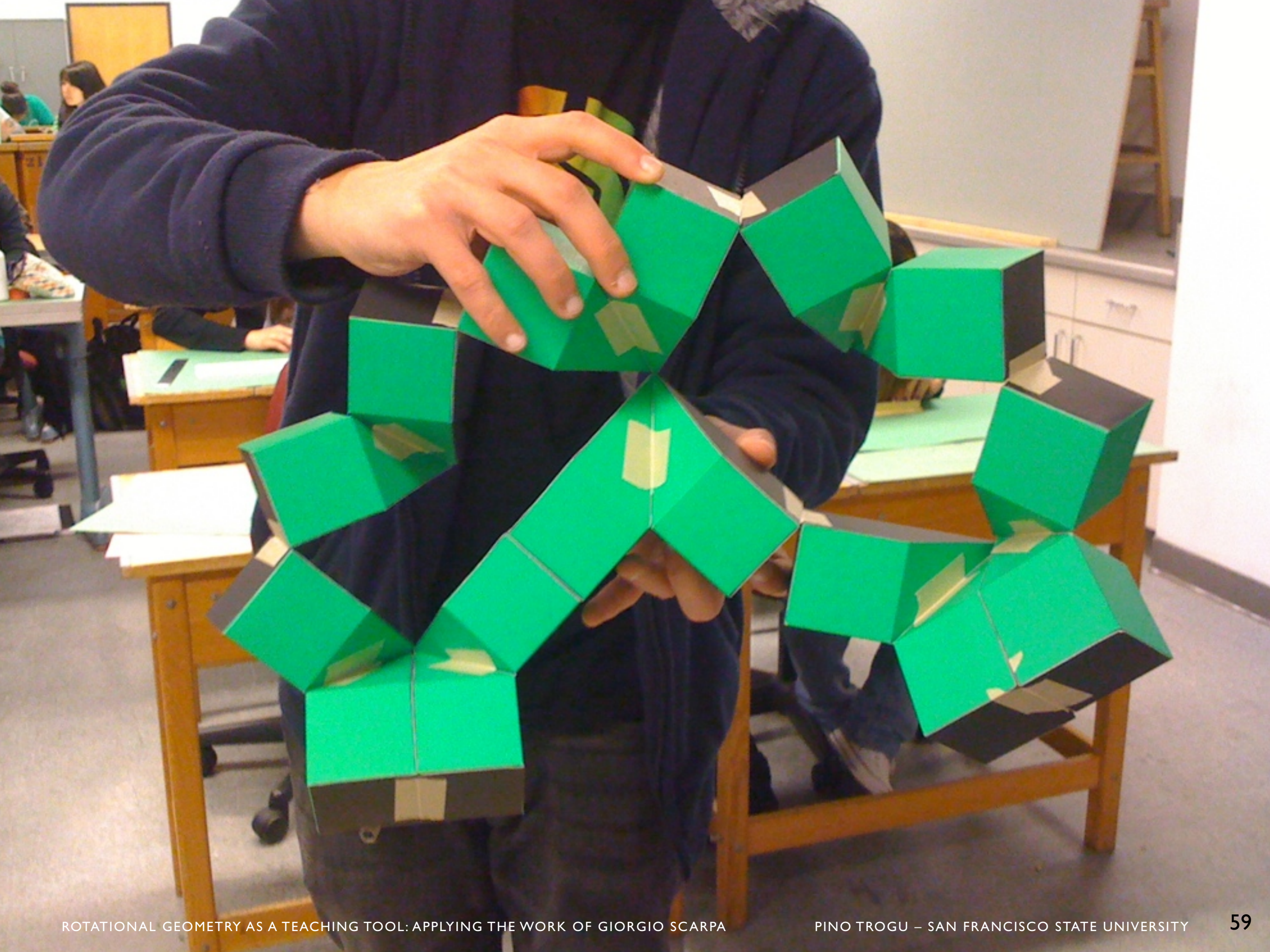














# REFERENCES & LINKS

Jürg Spiller, ed., *Paul Klee: The Thinking Eye*, trans. Ralph Manheim. Wittenborn, 1961.

Giorgio Scarpa, *Modelli di geometria rotatoria* [Models of rotational geometry]  
Zanichelli, 1978.

Erik D. Demaine and Joseph O'Rourke, *Geometric Folding Algorithms. Linkages, Origami, Polyhedra*. Cambridge University Press, 1997.

Cube Section [trogu.com/projects/getProject/20051225082001/project\\_html](http://trogu.com/projects/getProject/20051225082001/project_html)

Giorgio Scarpa [userwww.sfsu.edu/~trogu/scarpa](http://userwww.sfsu.edu/~trogu/scarpa)

PDF of slides and handouts

[trogu.com/Documents/conference/design-principles-and-practices](http://trogu.com/Documents/conference/design-principles-and-practices)

Contact

[trogu@sfsu.edu](mailto:trogu@sfsu.edu)    [design.sfsu.edu](http://design.sfsu.edu)    [trogu.com](http://trogu.com)

[go to first slide](#)

*Music: il nuotatore, Giovanni Allevi*